

CONTEXT c1

Context for a model of the Bosch switchc mini-pilot Michael Butler 16 May 2008

I represent the continuous input as a function from Time to Signal value. As a first approximation, I have modelled time and signal value as natural numbers.

so we have a constant input : $\text{NAT} \rightarrow \text{NAT}$

and $\text{input}(t)$ represents the value of the input signal at time t .

The SwitchOn and SwitchOff conditions are then defined in terms of the continuous input.

The discrete behaviour of the switch is defined in teh machine

CONSTANTS

input

RTH

FTH

CT

BT

RisingEdge

SwitchOnCond

FallingEdge

SwitchOffCond

AXIOMS

axm1 : $\text{input} \in \text{N} \rightarrow \text{N}$

input is a funtion from time to the range off..on

axm8 : $RTH \in \text{N}$

Rising threshold

axm7 : $FTH \in \text{N}$

Falling threshold

axm4 : $FTH < RTH$

axm9 : $CT \in \text{N}$

Cycle time

axm10 : $BT \in \text{N}$

Debounce time

axm5 : $CT < BT$

axm6 : $RisingEdge \subseteq \text{N}$

t in RisingEdge means rising edge detectable at time t

axm11 : $\forall t. t \geq CT \Rightarrow$

$(t \in RisingEdge \Leftrightarrow$
 $\text{input}(t) > RTH \wedge$
 $\text{input}(t - CT) < RTH)$

Time t represents a rising edge iff

the input at time t is higher than RTH and at time $t-CT$ the input was lower than RTH

axm2 : $SwitchOnCond \subseteq \text{N}$

t in SwitchOnCond means that teh swtch on condition holds at time t .

axm3 : $\forall t.$

$$\begin{aligned}
 & t \in \mathbb{N} \Rightarrow \\
 & (t \in \text{SwitchOnCond} \Leftrightarrow \\
 & (\exists t_0. t_0 \in \mathbb{N} \wedge t_0 < t \wedge \\
 & \quad t_0 \in \text{RisingEdge} \wedge \\
 & \quad t - t_0 \geq BT \wedge \\
 & \quad (\forall i. i \in t_0 .. t \Rightarrow \text{input}(i) > RTH) \\
 &) \\
 &)
 \end{aligned}$$

The switch on condition is true at time t iff

a rising edge was detected some time previously (t0) and the input exceeds RTH for BT after the rising edge

axm12 : $\text{FallingEdge} \subseteq \mathbb{N}$

axm14 : $\forall t. t \geq CT \Rightarrow$

$$\begin{aligned}
 & (t \in \text{FallingEdge} \Leftrightarrow \\
 & \text{input}(t) < FTH \wedge \\
 & t - CT \in \mathbb{N} \wedge \text{input}(t - CT) > FTH)
 \end{aligned}$$

Time t represents a rising edge iff

the input is lower than FTH and at time t-CT the input was greater than FTH

axm13 : $\text{SwitchOffCond} \subseteq \mathbb{N}$

axm15 : $\forall t. t \in \mathbb{N} \Rightarrow$

$$\begin{aligned}
 & (t \in \text{SwitchOffCond} \Leftrightarrow \\
 & (\exists t_0. t_0 \in \mathbb{N} \wedge t_0 < t \wedge \\
 & \quad t_0 \in \text{FallingEdge} \wedge \\
 & \quad t - t_0 \geq BT \wedge \\
 & \quad (\forall i. i \in t_0 .. t \Rightarrow \text{input}(i) < FTH) \\
 &) \\
 &)
 \end{aligned}$$

The switch off condition is true at time t iff

a falling edge was detected some time previously (t0) and the input is lower than RTH for BT after the falling edge

END