

SHEP Seminars
Southampton University
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ν in cosmology: current bounds and new physics scenarios

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IPPP, Durham University



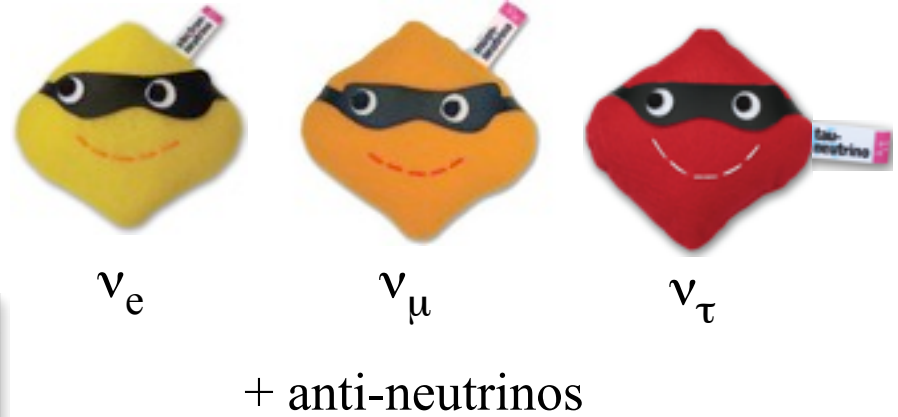
Contents

- ✓ 3ν scenario & Early Universe
 - ✓ Neutrino proprieties from cosmological probes
- ✓ Extended scenario: sterile neutrinos
 - ✓ Formalism and EoM for active-sterile evolution
 - ✓ cosmological bounds after Planck data
 - ✓ new physics scenarios
- ✓ Conclusions

3 ν Scenario

The Standard Model includes 3 species of massless neutrinos interacting only through the weak interactions.

LEP data: $N_\nu = 2.984 \pm 0.008$
(PDG 2012)

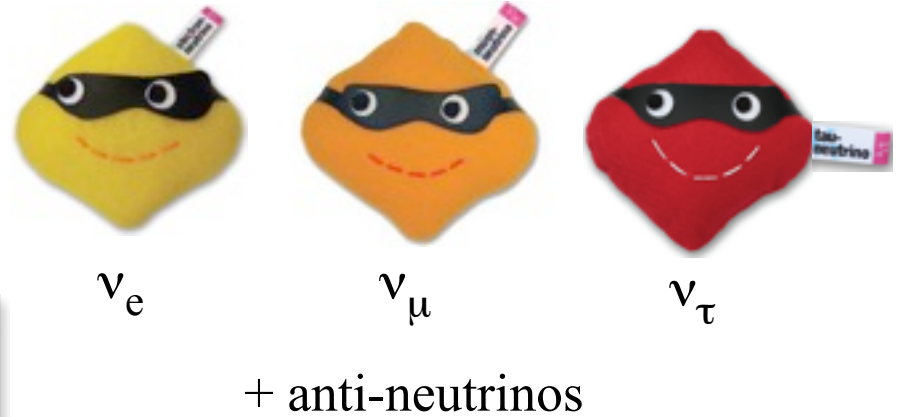


3ν Scenario + Oscillations (I)

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In the last two decades, a long series of **ν oscillation experiments** has established that neutrinos ***are massive and oscillate***.

Indeed the 3-flavour eigenstates (ν_e, ν_μ, ν_τ) produced by charged-current weak interactions oscillate due to the fact that they are quantum superposition of the 3-mass eigenstates (ν_1, ν_2, ν_3):

$$|\nu_\alpha\rangle = \sum_i U_{\alpha i}^* |\nu_i\rangle$$

flavour eigenstates flavour eigenstates



3ν Scenario + Oscillations (II)

Pontecorvo-Maki-Nakagawa-Sakata (PMNS) matrix:

$$U = \begin{pmatrix} 1 & 0 & 0 \\ 0 & c_{23} & s_{23} \\ 0 & -s_{23} & c_{23} \end{pmatrix} \begin{pmatrix} c_{13} & 0 & s_{13}e^{-i\delta_{CP}} \\ 0 & 1 & 0 \\ -s_{13}e^{i\delta_{CP}} & 0 & c_{13} \end{pmatrix} \begin{pmatrix} c_{12} & s_{12} & 0 \\ -s_{12} & c_{12} & 0 \\ 0 & 0 & 1 \end{pmatrix} \begin{pmatrix} 1 & 0 & 0 \\ 0 & e^{i\beta} & 0 \\ 0 & 0 & e^{i\gamma} \end{pmatrix}$$

$$s_{ij} = \sin \theta_{ij}, \quad c_{ij} = \cos \theta_{ij}$$

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Parameters well-known from oscillation experiments:

- ✓ mixing angles $\theta_{23} \approx 39^\circ$, $\theta_{13} \approx 9^\circ$, $\theta_{12} \approx 34^\circ$
- ✓ oscillations driven by 2 independent mass squared differences

$$\Delta m_{21}^2 = \Delta m_{\text{sol}}^2 = 7.5 \times 10^{-5} \text{ eV}^2, \quad |\Delta m_{31,2}^2| = |\Delta m_{\text{atm}}^2| = 2.4 \times 10^{-3} \text{ eV}^2$$

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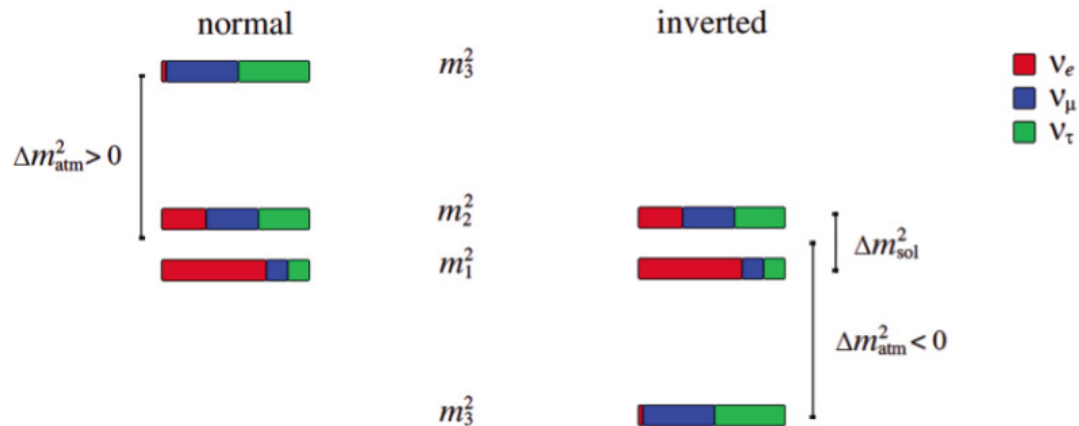
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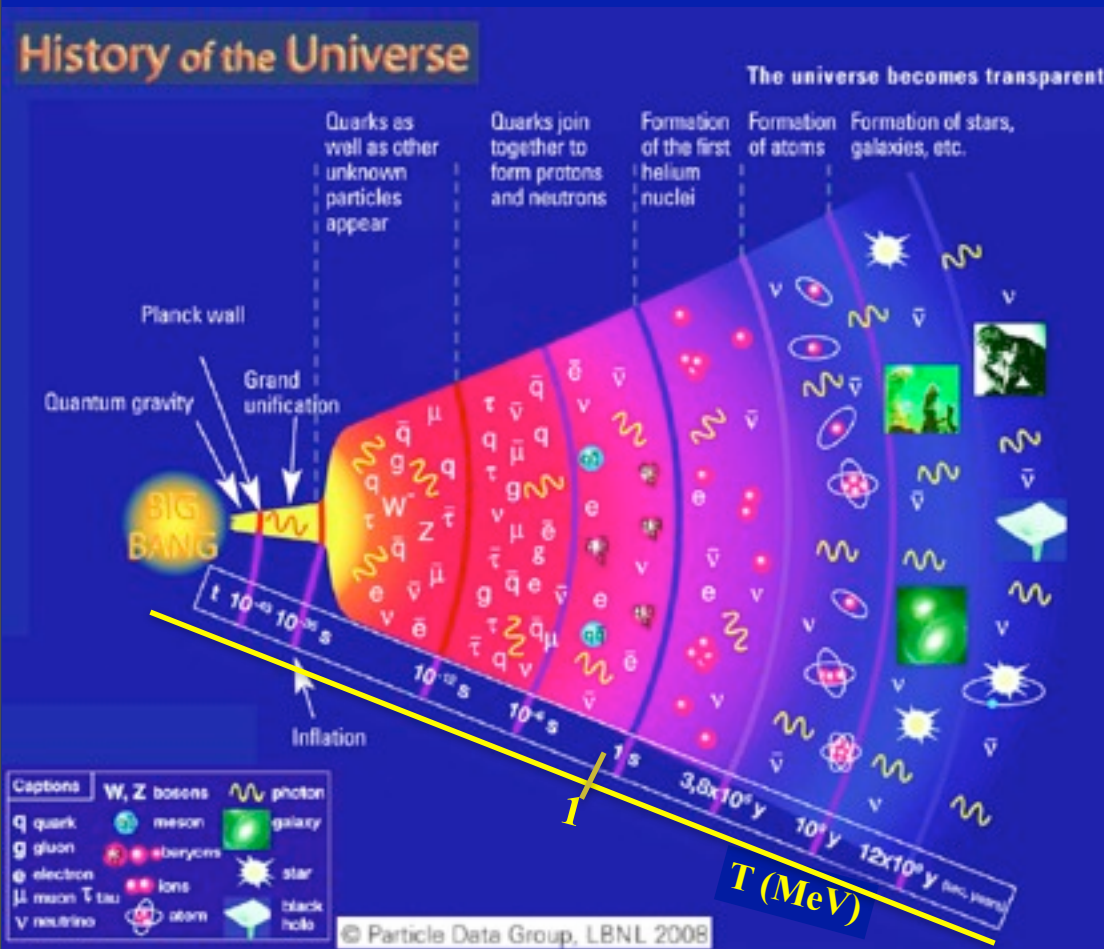
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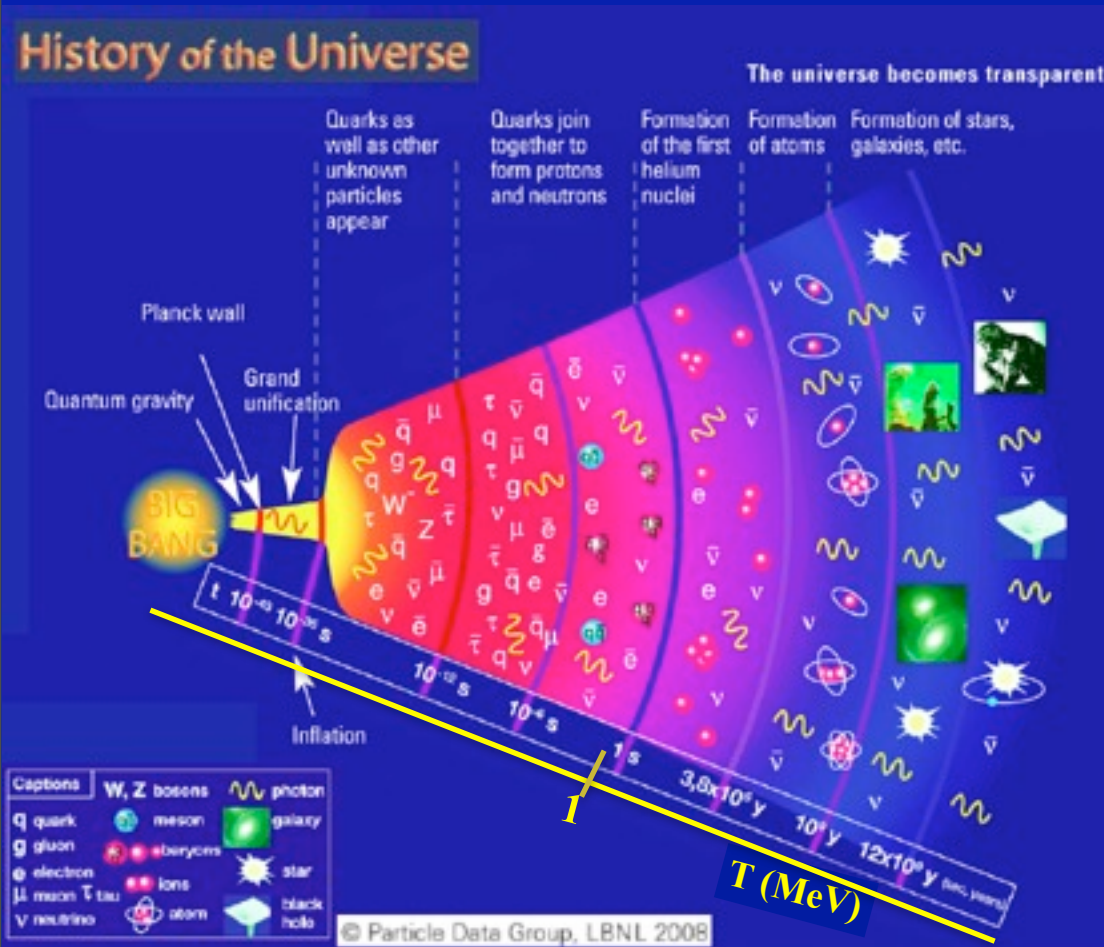
Still unknown: δ_{CP} and the *neutrino hierarchy* (i.e. the sign of Δm_{atm}^2):



ν in the Early Universe (I)

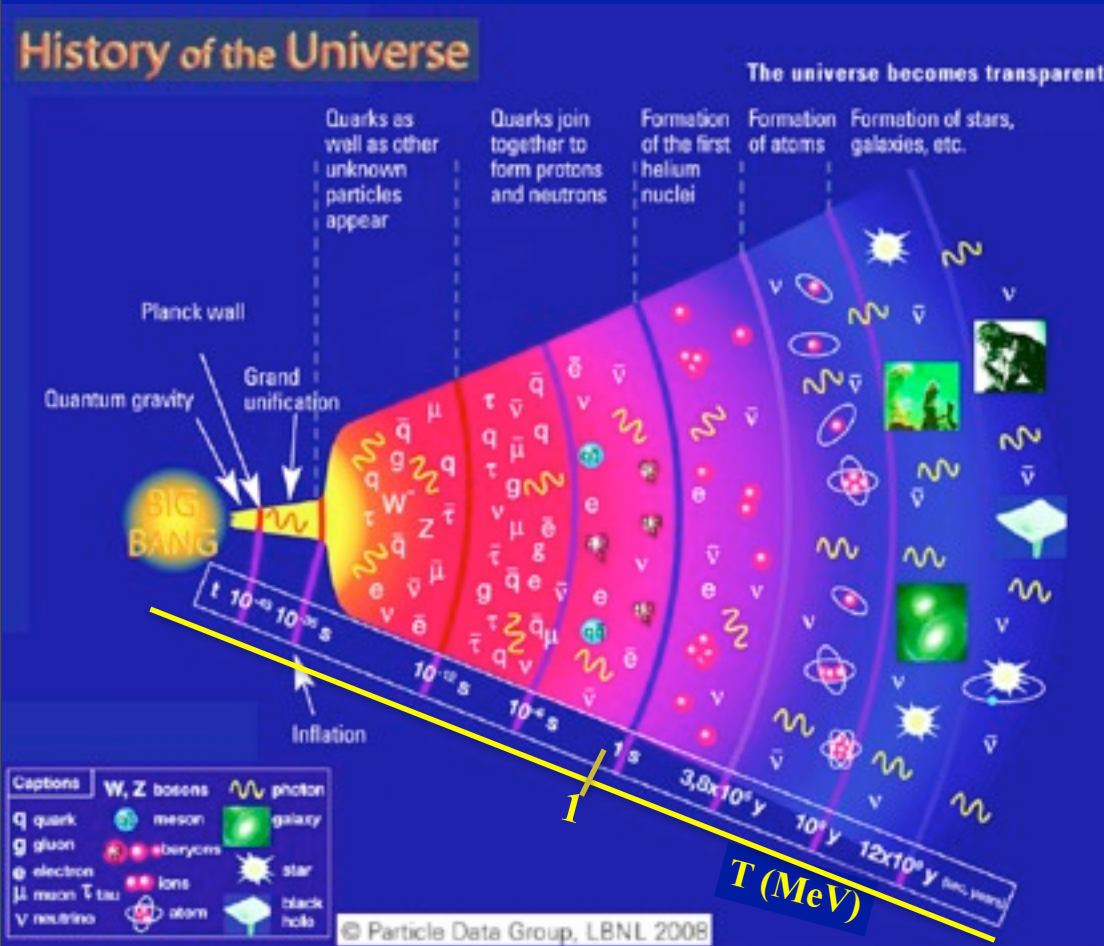


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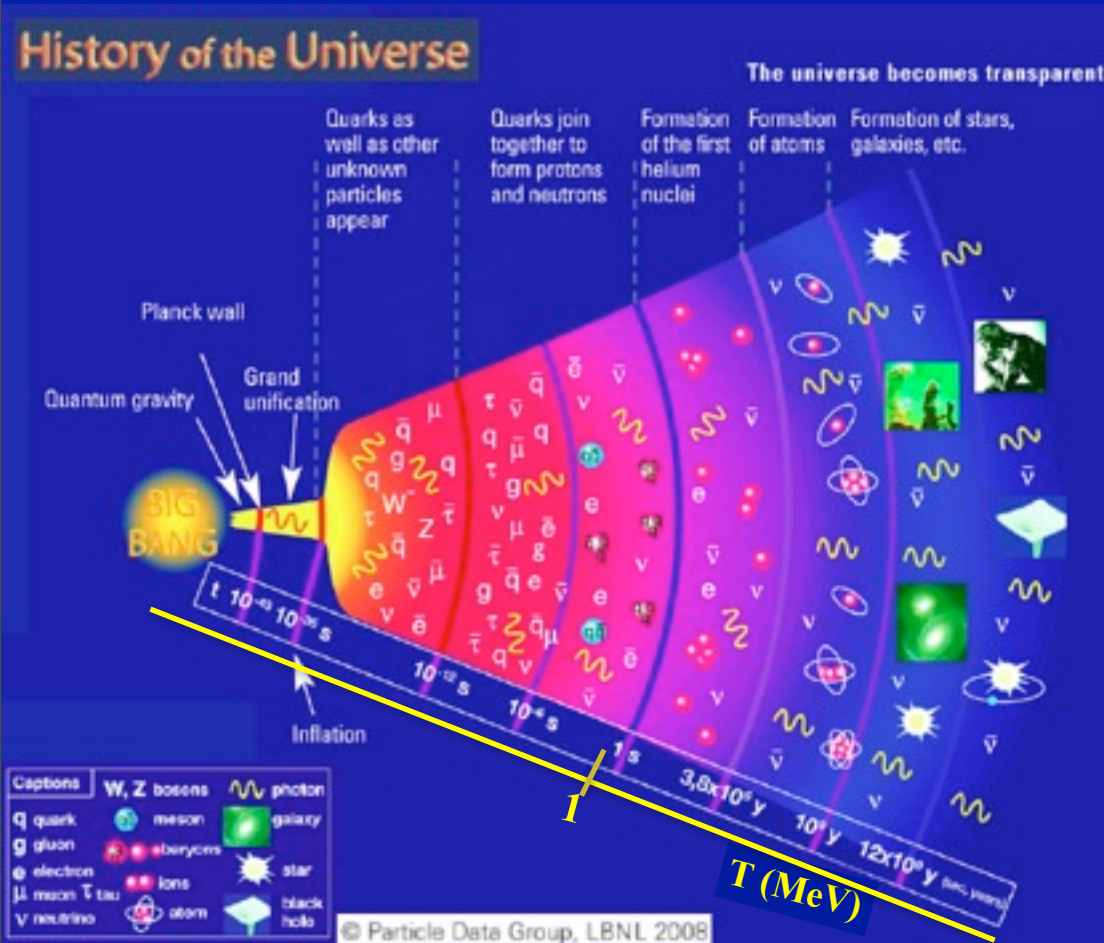
- $T_d \sim 1 \text{ MeV}$ (1 sec): $\Gamma_{\text{WK}}(T_d) = H(T_d)$



ν decoupling by weak interactions with the primordial plasma \rightarrow CNB

(Cosmic Neutrino Background)

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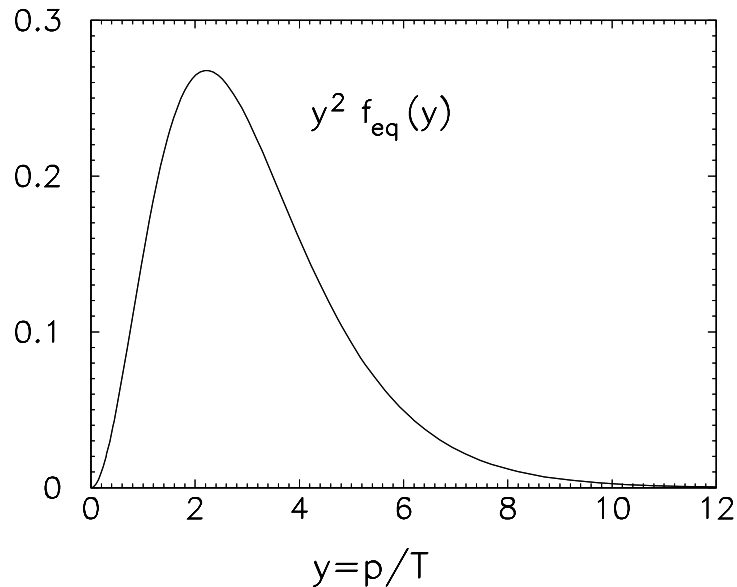
(Cosmic Neutrino Background)

CNB contributes to radiation at early times and to matter at late times

- * Thermal distribution: $T_\nu = 1.95 \text{ K}$
- * Number density ($\nu + \bar{\nu}$): $112 \text{ cm}^{-3}/\text{flavour}$
- * Mean kinetic energy: $\ll \text{meV}$
- * Energy density ($m > T$): $\Omega_\nu h^2 = \frac{\sum_i m_i}{94.1 \text{ eV}}$

BBN	CMB	LSS
$T \sim 0.8 \text{ MeV}$		$T < \text{eV}$
ν flavour sensitivity		ν mass sensitivity
N_{eff}		N_{eff}

ν in the Early Universe (II)



Neutrinos mass < 1 eV \rightarrow still ultra-relativistic at the decoupling



Neutrinos keep **a momentum spectrum with an equilibrium Fermi-Dirac form with temperature T**

$$f_{eq}(p, T) = \frac{1}{e^{p/T} + 1}$$

- In the **standard cosmological scenario**, neutrinos of different flavours are produced with the same energy spectrum (except for small spectral distortions due to a non-instantaneous neutrino decoupling)



no effect from the oscillations among the 3 flavour states in the standard scenario.

- **In non-standard scenarios** (primordial neutrino asymmetry, sterile neutrinos, low reheating)

\rightarrow Oscillations can lead to cosmological consequences, depending on the temperature

Radiation Content in the Universe

At $T < m_e$, the radiation content of the Universe is

$$\varepsilon_R = \varepsilon_\gamma + \varepsilon_\nu + \varepsilon_x$$

The **non-e.m.** energy density is parameterized by the effective numbers of neutrino species N_{eff}

$$\varepsilon_\nu + \varepsilon_x = \frac{7}{8} \frac{\pi^2}{15} T_\nu^4 N_{\text{eff}} = \frac{7}{8} \frac{\pi^2}{15} T_\nu^4 (N_{\text{eff}}^{\text{SM}} + \Delta N)$$

$N_{\text{eff}}^{\text{SM}} = 3.046$ due to non-instantaneous neutrino decoupling
(+ oscillations)

Mangano et al. 2005

$\Delta N =$ Extra Radiation: axions and axion-like particles, **sterile neutrinos (totally or partially thermalized)**, neutrinos in very low-energy reheating scenarios, relativistic decay products of heavy particles...

Di Bari et al. 2013, Boehm et al. 2012, Conlon and Marsh, 2013, Gelmini, Palomarez-Ruiz, Pascoli, 2004

Big Bang Nucleosynthesis

Big Bang Nucleosynthesis (BBN) is the epoch of the Early Universe ($T \sim 1 - 0.01$ MeV) when the primordial abundances of light elements were produced, in particular ${}^2\text{H}$, ${}^3\text{He}$, ${}^4\text{He}$, ${}^7\text{Li}$.

When $\Gamma_{n \leftrightarrow p} < H \rightarrow$ *neutron-to-proton ratio* $\frac{n_n}{n_p} = \frac{n}{p} = e^{-\Delta m/T}$ *freezes out*
 $\rightarrow 1/7$ including neutron decays

This ratio fixes the primordial yields, especially the ${}^4\text{He}$ abundance characterized by

$$Y_p = \frac{2n/p}{1 + n/p}$$

Helium mass fraction

Abundance of light elements predicted as function of:

- standard scenario: $\omega_b = \Omega_b h^2$
(equivalently $\eta_B = n_B/n_\gamma$)
- non-standard: $\omega_b = \Omega_b h^2$
 $N_{\text{eff}} (> 3)$
 ξ_ν (chemical potential)

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BBN code: PArthENoPE (Pisanti et al, 2008)
numerical solution of a set of differential equations governing the evolution of each nuclide species

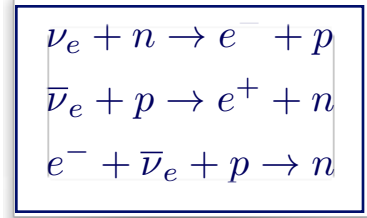
- weak rates (known at 0.1% level)
- neutron lifetime τ_n ($= 880.1 \pm 1.1$ s; *PDG 2012*)
- nuclear rates

ν and Big Bang Nucleosynthesis

Cosmological ν influence the production of primordial light elements in two ways:

1) $\nu_e, \bar{\nu}_e$ participate in the CC weak interactions which rule the $n \leftrightarrow p$ interconversion

any change in their energy spectra can shift the n/p ratio
freeze out temperature \Rightarrow modification in the primordial yields



i.e. $\nu_e - \bar{\nu}_e$ asymmetry (chemical potential ξ_e) $\rightarrow \frac{n}{p} = e^{(-\Delta m/T - \xi_e)}$

2) ν_α contribute to the radiation energy density that governs the expansion rate of the Universe before and during BBN epoch and then the n/p ratio.

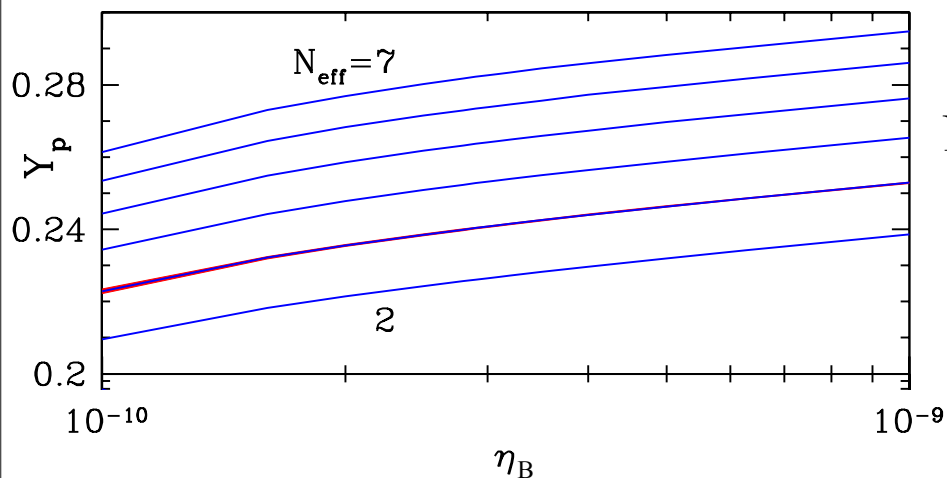
$$H = \frac{\dot{a}}{a} = \sqrt{\frac{8\pi G_N \epsilon_R}{3}}$$

(γ, e, ν, x)
 $\hookrightarrow \propto N_{\text{eff}}$

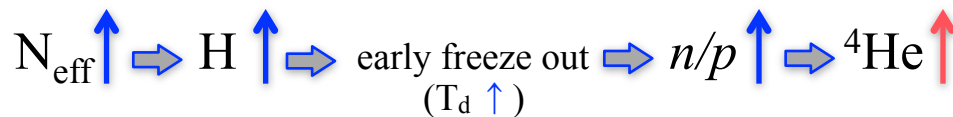
Changing the H would alter the n/p ratio at the onset of BBN and hence the light element abundances

Extra radiation impact on BBN and constraints

Light element abundances are sensitive to extra radiation:



Adapted from *Cyburt et al, 2002*



Upper limit on N_{eff} from constrains on primordial yields of D and ${}^4\text{He}$:

No strong indication for $\Delta N_{\text{eff}} > 0$ from BBN alone

$$\Delta N_{\text{eff}} \leq 1 \quad (95\% \text{ C.L.})$$

Hamann et al, 2011

Mangano and Serpico, 2012

From new precise measure of D in damped Lyman- α system

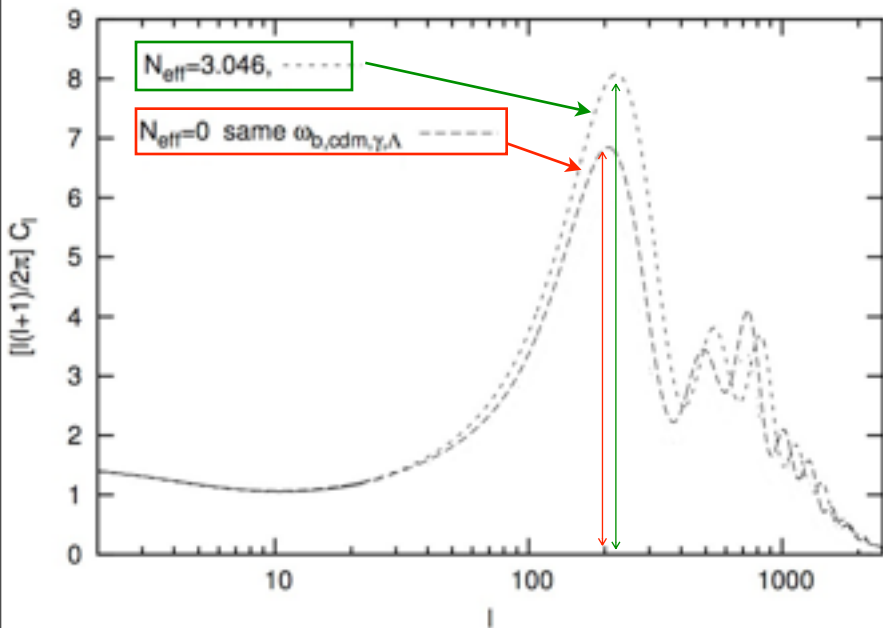
$$N_{\text{eff}} = 3.28 \pm 0.28$$

Cooke, Pettini et al., 2013

1 extra d.o.f. ruled out at 99.3 C.L.

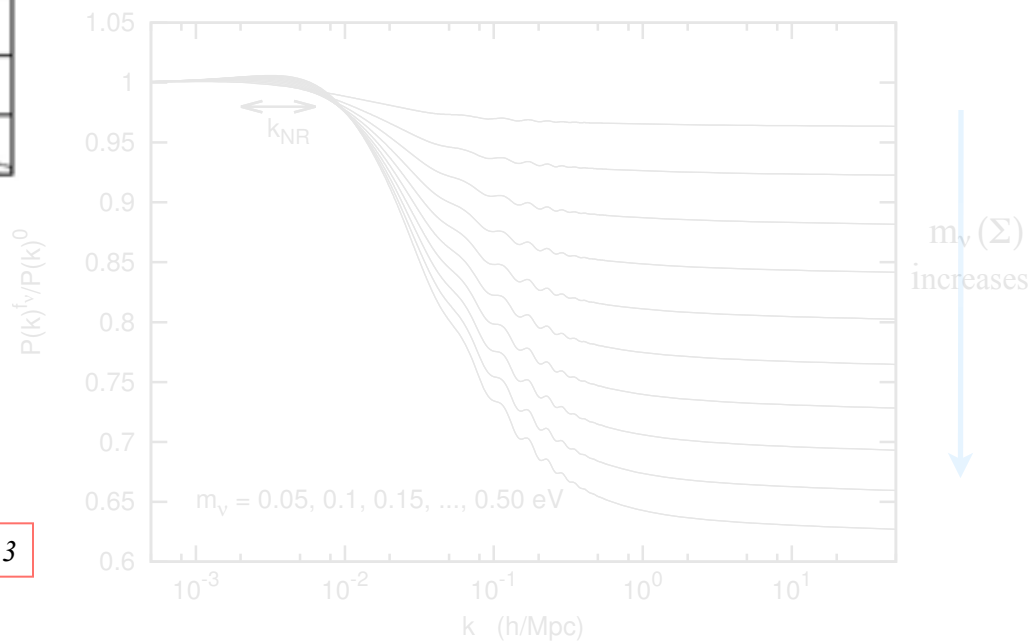
ν and CMB and LSS

ν 's and their masses effect the PS of temperature fluctuations of CMB ($T < eV$) and the matter PS of the LSS inferred by the galaxy surveys.



N_{eff} and m_ν affect the time of *matter-radiation equality*
 → consequences on the amplitude of the first peak and on the peak locations

$$1 + z_{\text{eq}} = \frac{\omega_m}{\omega_\gamma} \frac{1}{1 + 0.227 N_{\text{eff}}}$$

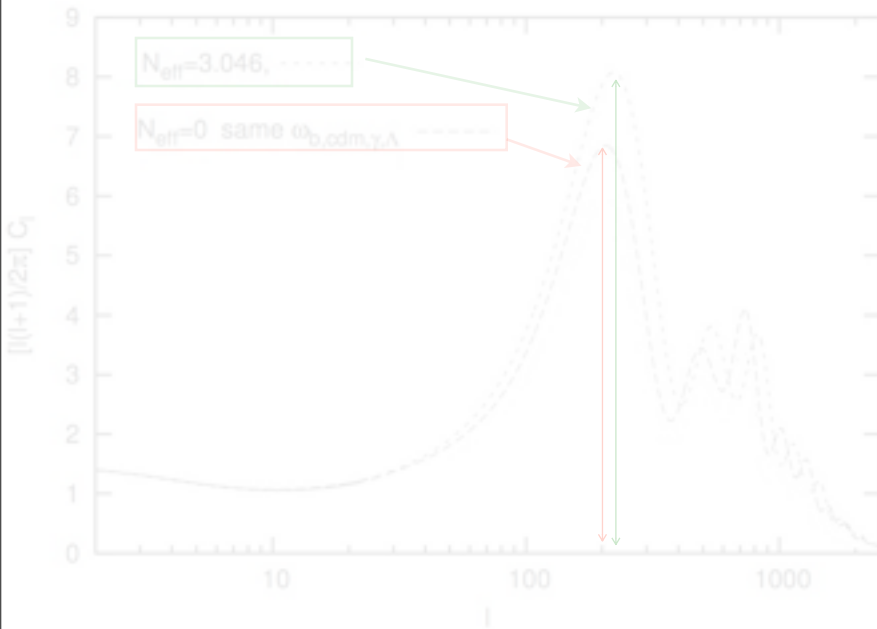


Taken from

Lesgourgues, Mangano, Miele and Pastor "Neutrino Cosmology", 2013

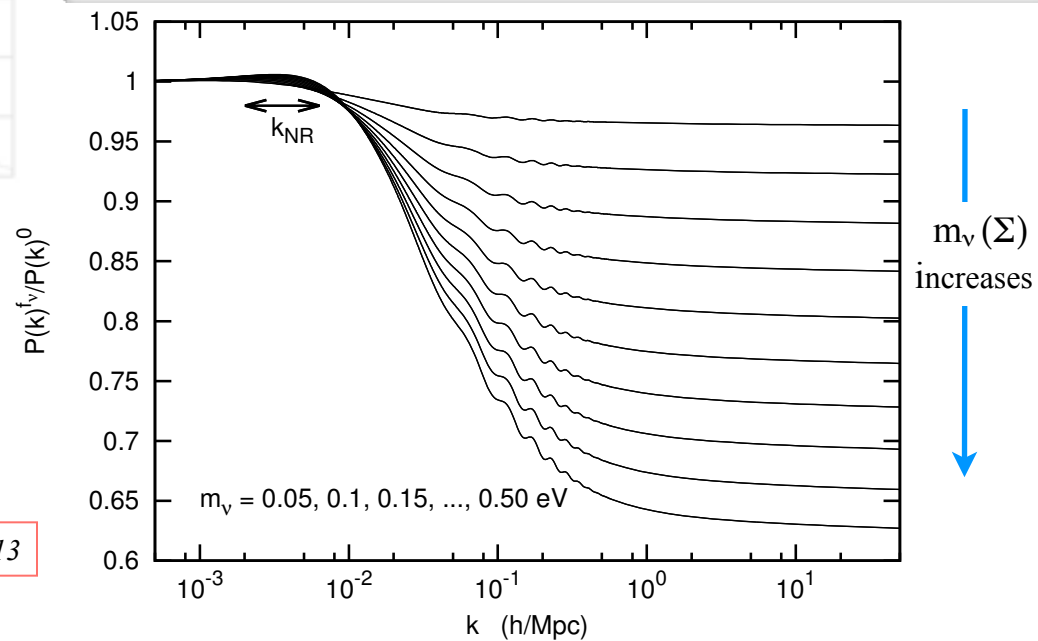
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The small-scale matter power spectrum $P(k > k_{nr})$ is reduced in presence of massive ν :

- ✓ free-streaming neutrinos do not cluster
- ✓ slower growth rate of CDM (baryon) perturbations



Taken from

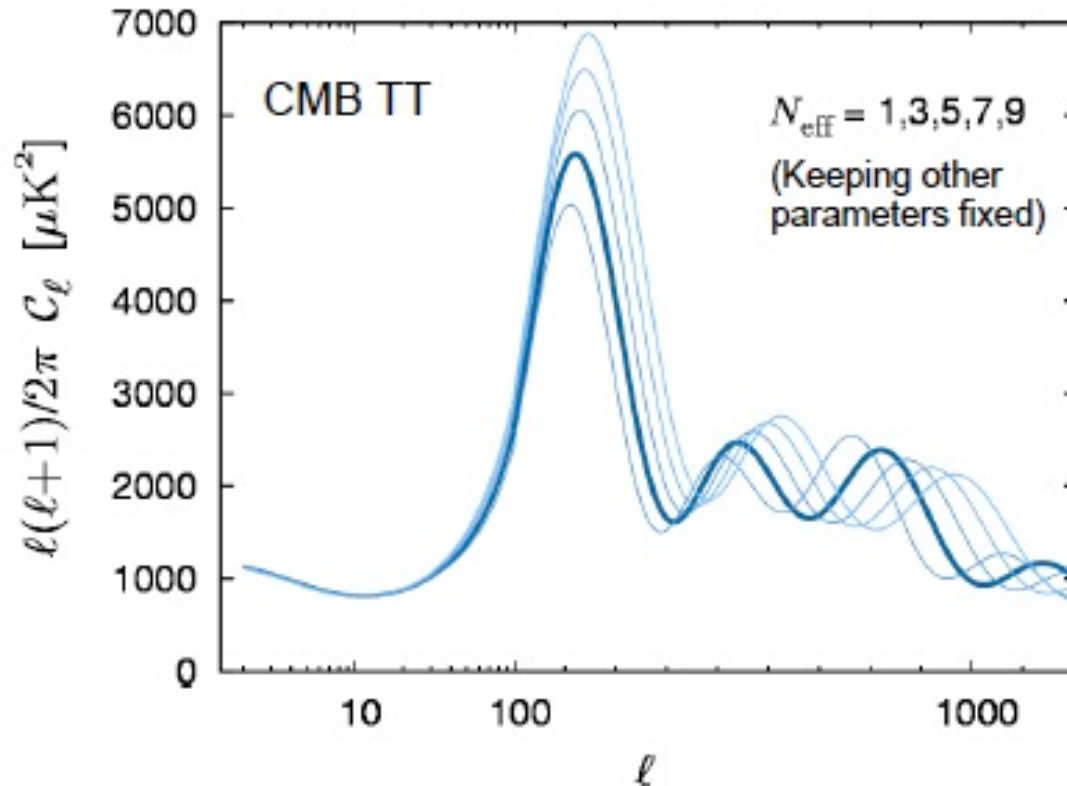
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Extra radiation impact on CMB

If additional degrees of freedom are still relativistic at the time of CMB formation, they impact the CMB anisotropies.



constraints N_{eff} from the
CMB Spectrum

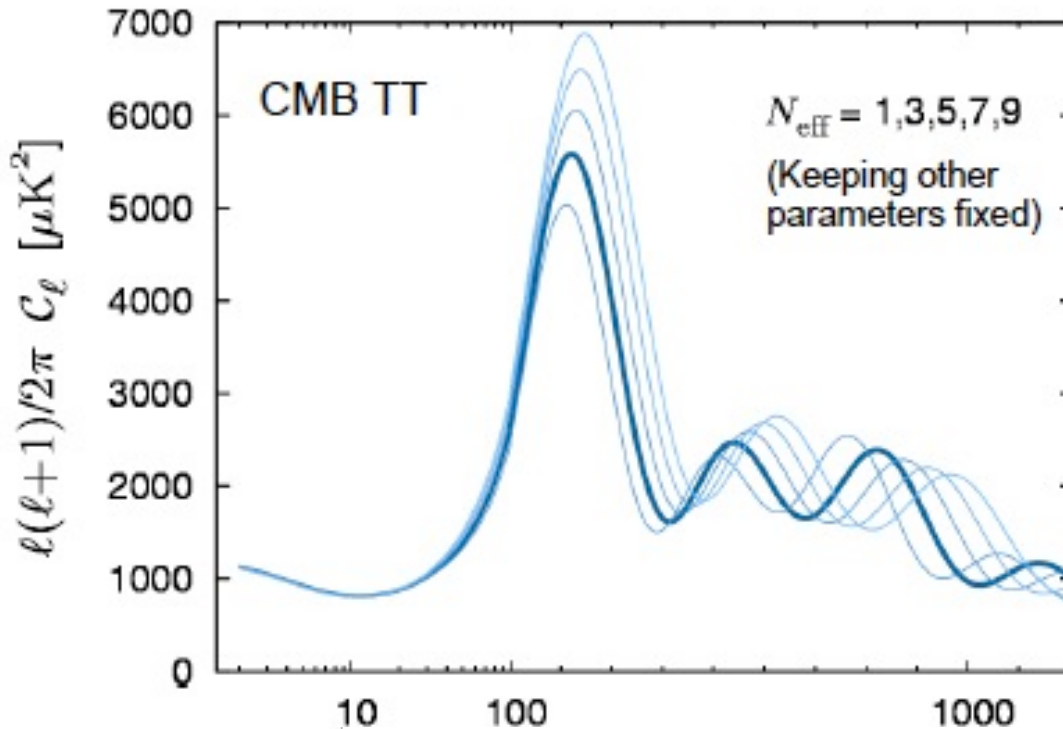


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constraints N_{eff} from the CMB Spectrum



Same data used to measure other cosmological parameters

basic parameters of Λ CDM:

$$(\Omega_b h^2, \Omega_c h^2, 100\theta_{MC}, n_s, A_s, \tau)$$

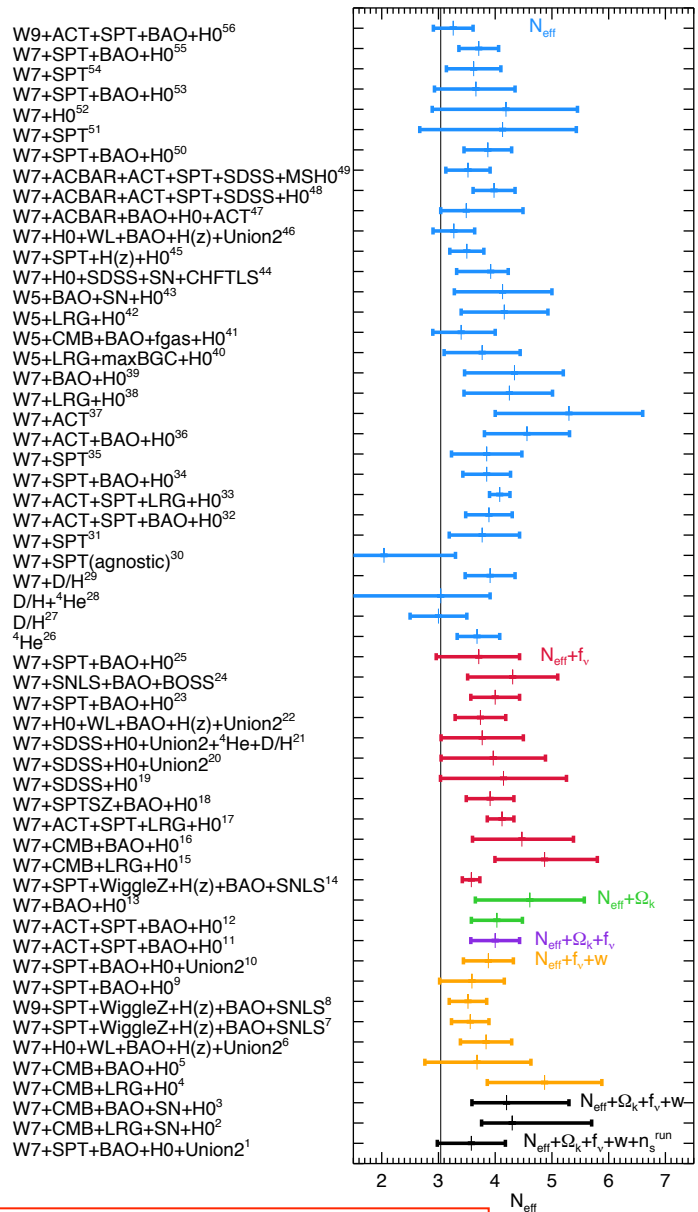
+ derived parameters

$$(H_0, \Omega_k, \Omega_\Lambda, N_{\text{eff}}, \sigma_8, \sum m_\nu, z_{re}, Y_p, w, \Omega_m z_{LS} \dots)$$

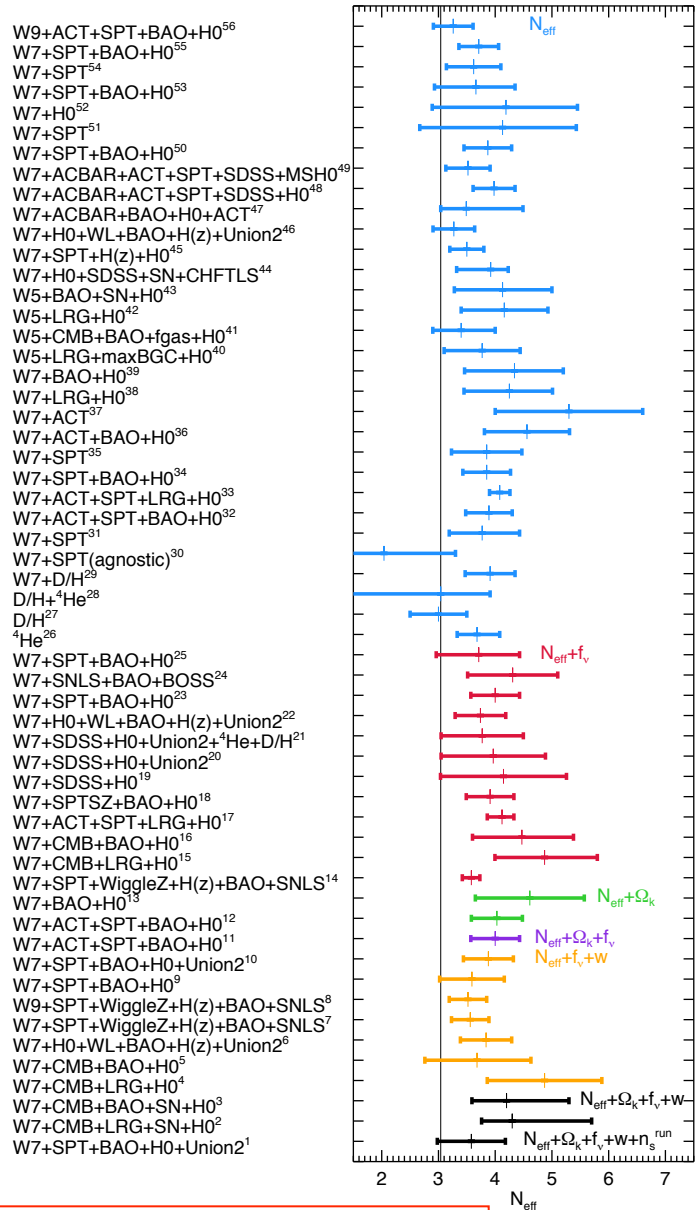
→ *degeneracies*

→ *necessary to combine with other cosmological probes*

CMB & LSS hints for extra radiation before Planck



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Summarizing:

CMB (combined)	N_{eff}
WMAP5+ BAO+ H0+SN	4.4 ± 1.5 (68% C.L.)
WMAP7+ BAO+ H0	4.4 ± 0.84 (68% C.L.)
WMAP9+ BAO+ H0+ ACT+ SPT (Y_p fixed)	3.84 ± 0.40 (68% C.L.)

Komatsu et al., 2008,2010

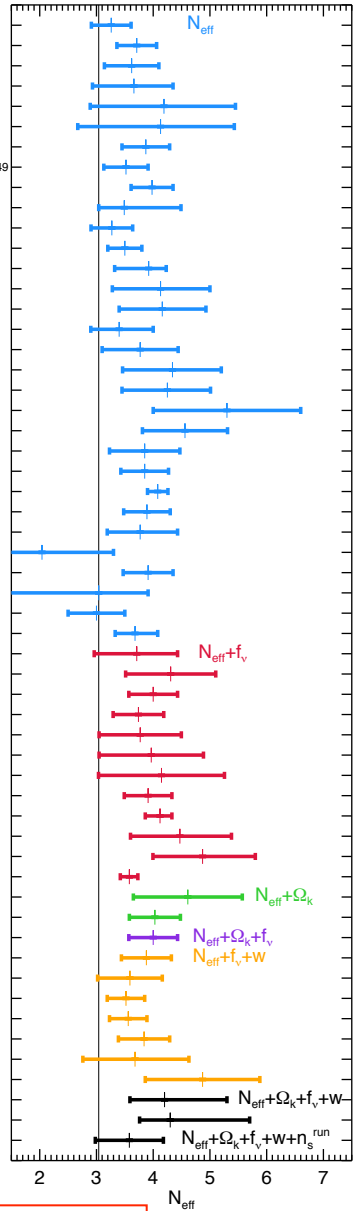
G. Hinshaw, et al.2013

J.L.Sievers et al. 2013

Riemer-Sørensen, Parkinson & Davis, 2013

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W9+ACT+SPT+BAO+H0⁵⁶
 W7+SPT+BAO+H0⁵⁵
 W7+SPT⁵⁴
 W7+SPT+BAO+H0⁵³
 W7+H0⁵²
 W7+SPT⁵¹
 W7+SPT+BAO+H0⁵⁰
 W7+ACBAR+ACT+SPT+SDSS+MSH0⁴⁹
 W7+ACBAR+ACT+SPT+SDSS+H0⁴⁸
 W7+ACBAR+BAO+H0+ACT⁴⁷
 W7+H0+WL+BAO+H(z)+Union2⁴⁶
 W7+SPT+H(z)+H0⁴⁵
 W7+H0+SDSS+SN+CHFTLS⁴⁴
 W5+BAO+SN+H0⁴³
 W5+LRG+H0⁴²
 W5+CMB+BAO+fgas+H0⁴¹
 W5+LRG+maxBGC+H0⁴⁰
 W7+BAO+H0³⁹
 W7+LRG+H0³⁸
 W7+ACT³⁷
 W7+ACT+BAO+H0³⁶
 W7+SPT³⁵
 W7+SPT+BAO+H0³⁴
 W7+ACT+SPT+LRG+H0³³
 W7+ACT+SPT+BAO+H0³²
 W7+SPT³¹
 W7+SPT(agnostic)³⁰
 W7+D/H²⁹
 D/H+⁴He²⁸
 D/H²⁷
⁴He²⁶
 W7+SPT+BAO+H0²⁵
 W7+SNLS+BAO+BOSS²⁴
 W7+SPT+BAO+H0²³
 W7+H0+WL+BAO+H(z)+Union2²²
 W7+SDSS+H0+Union2+⁴He+D/H²¹
 W7+SDSS+H0+Union2²⁰
 W7+SDSS+H0¹⁹
 W7+SPTSZ+BAO+H0¹⁸
 W7+ACT+SPT+LRG+H0¹⁷
 W7+CMB+BAO+H0¹⁶
 W7+CMB+LRG+H0¹⁵
 W7+SPT+WiggleZ+H(z)+BAO+SNLS¹⁴
 W7+BAO+H0¹³
 W7+ACT+SPT+BAO+H0¹²
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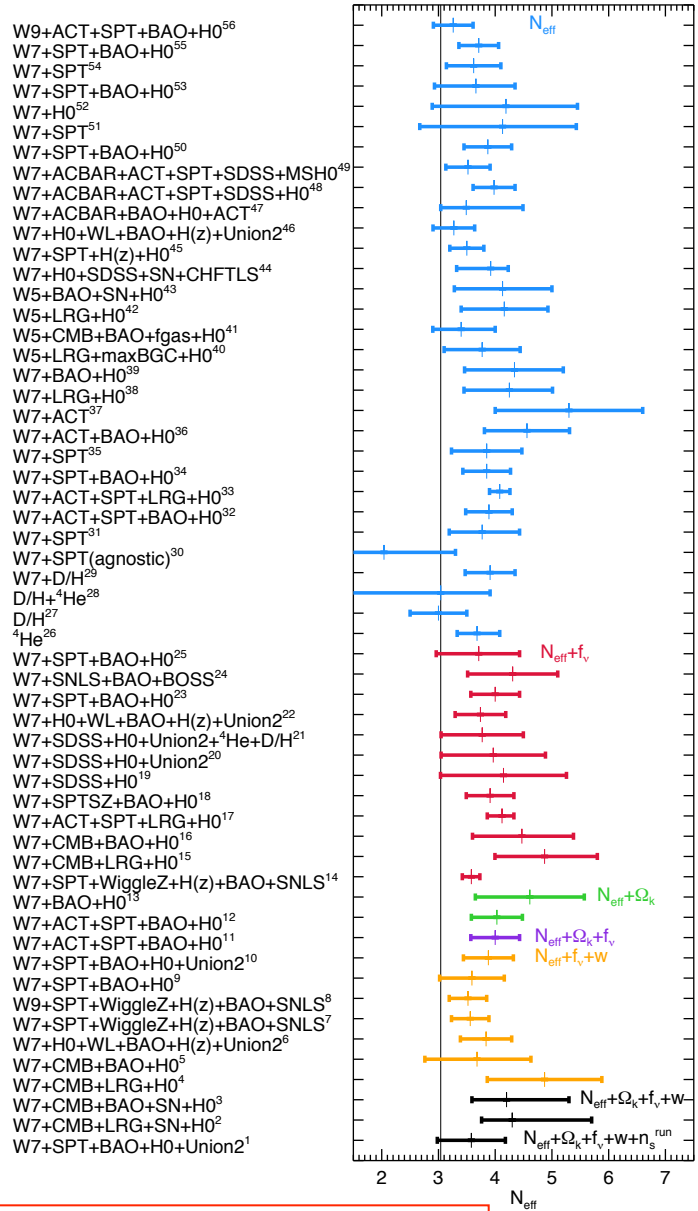
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Hints for extra radiation reduce over the years

Slight preference for $N_{\text{eff}} > 3.046$

N_{eff} and Σm_ν constraints after Planck (first release)



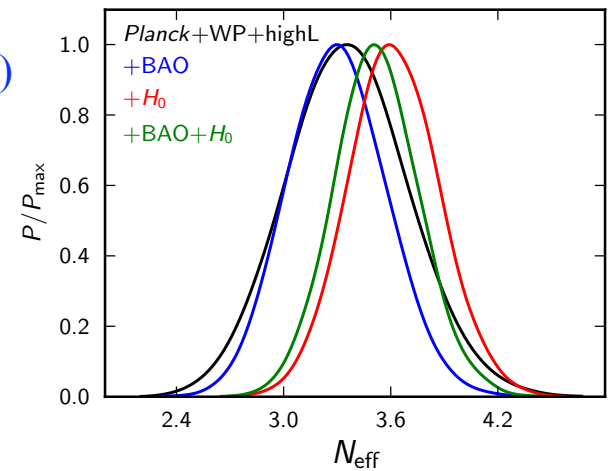
Standard scenario:

- $N_{\text{eff}} = 3.30 \pm 0.54$ (95 % C.L.; Planck+WP+highL+BAO)

↪ compatible with the standard value at $1-\sigma$

- For 3 degenerate active ν :

$$\Sigma m_\nu < 0.23 \text{ eV} \quad (95 \% \text{ C.L.; Planck+WP+highL+BAO})$$



Planck XVI, 2013

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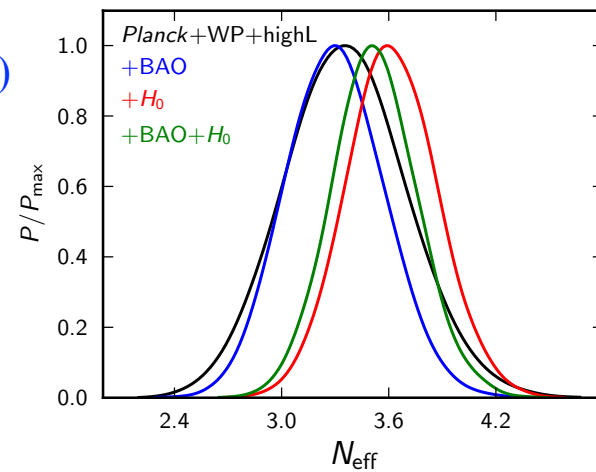
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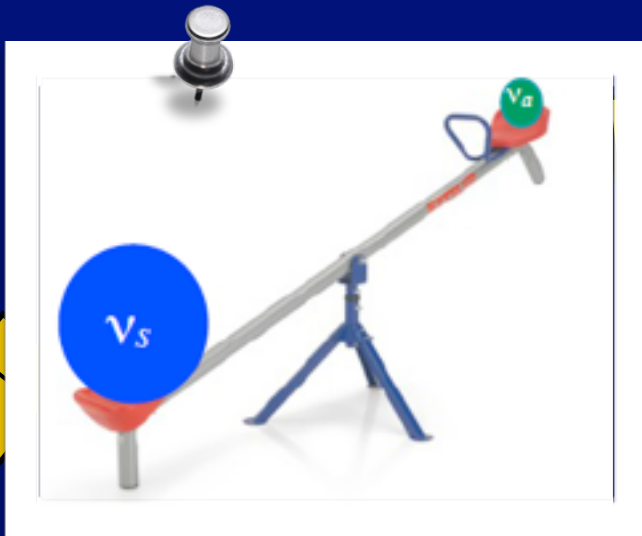
Second release to appear very soon....

only rumors from conference presentations...

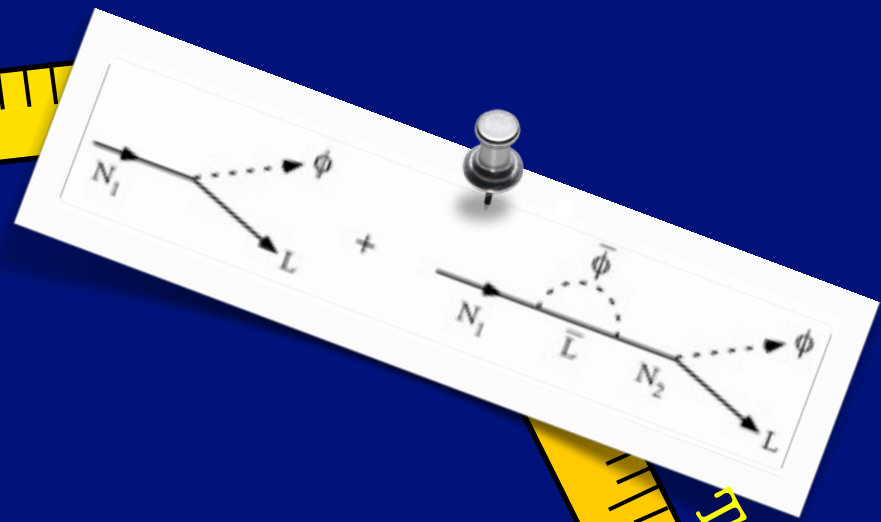
*Extended scenario:
sterile neutrinos*



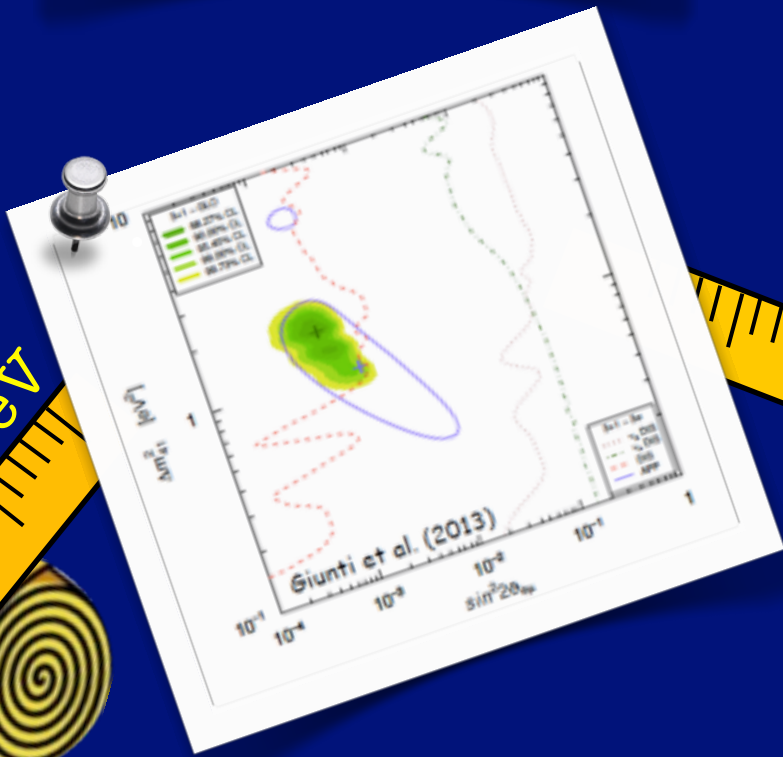
Sterile Neutrinos



M_{GUT}

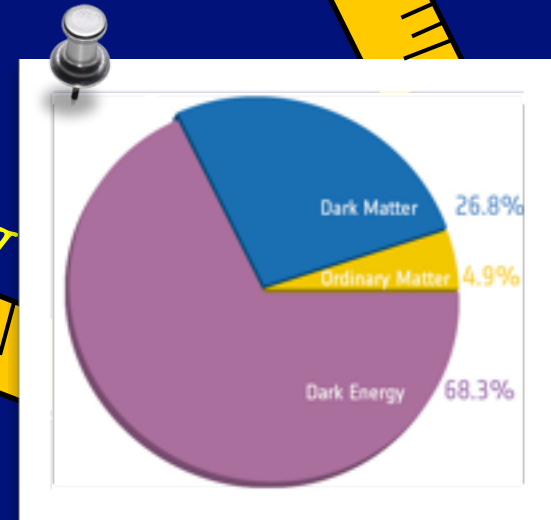


TeV



eV

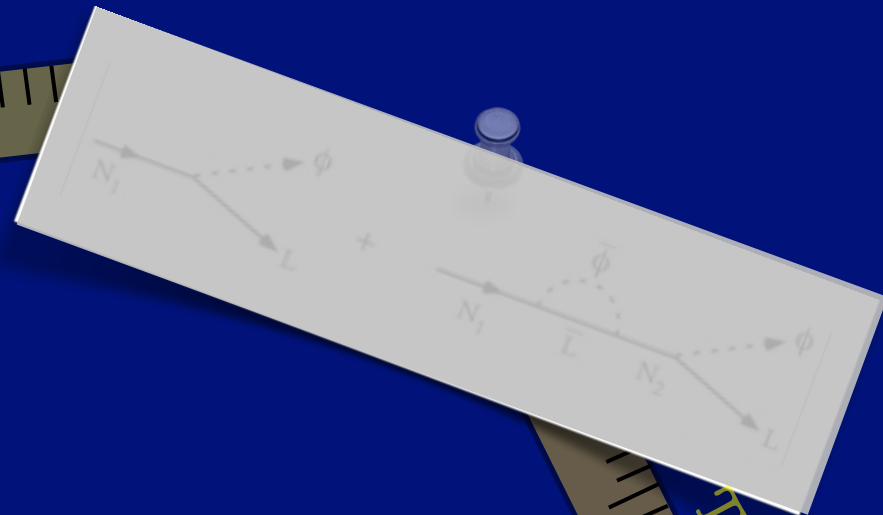
keV



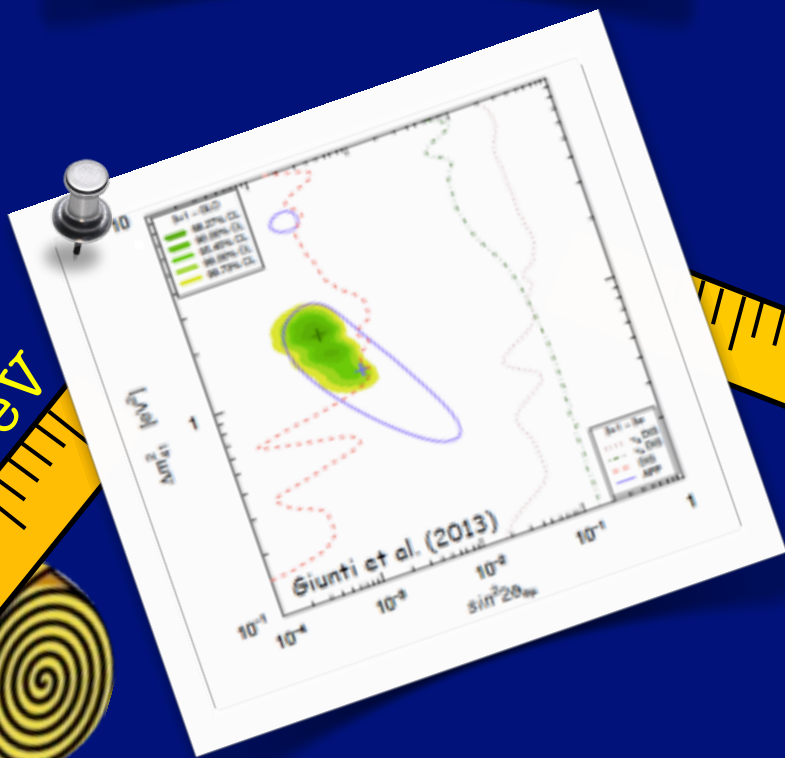
Sterile Neutrinos



M_{GUT}

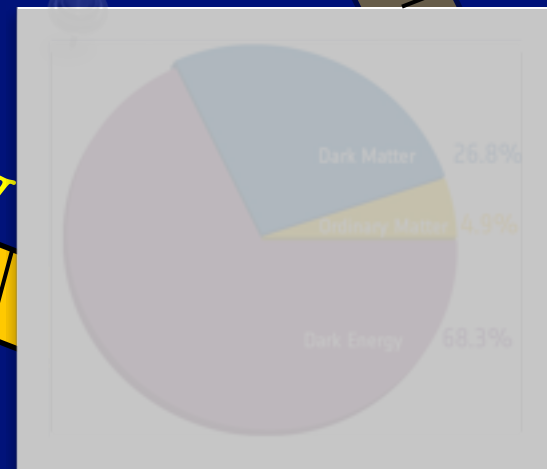


TeV

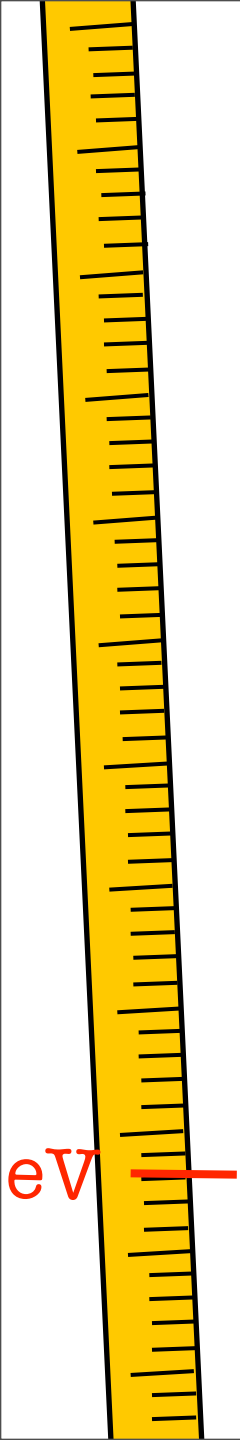


eV

keV



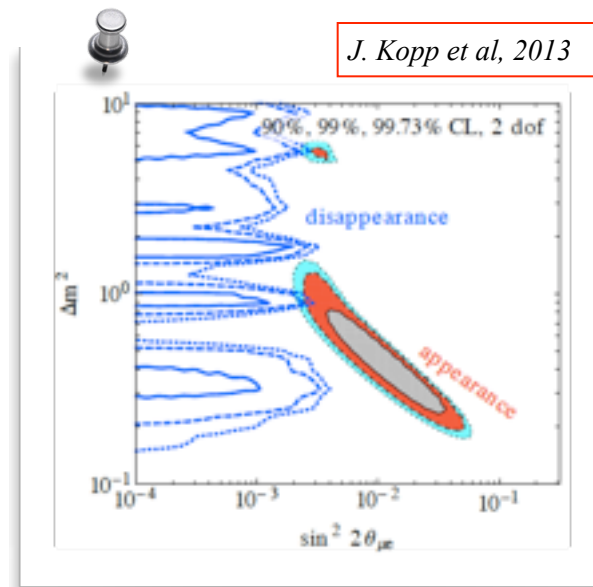
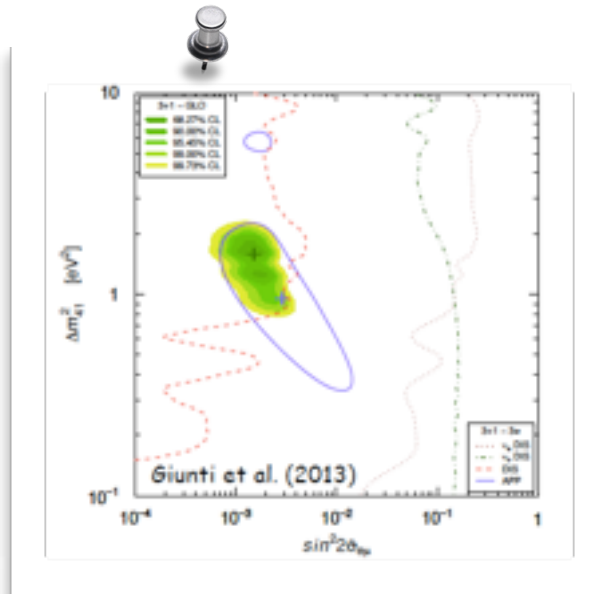
eV Sterile Neutrino



eV Sterile Neutrino

The investigation on Light Sterile Neutrinos has been stimulated by the presence of anomalous results from neutrino oscillation experiments

-  LNSD
-  MiniBooNE
-  Gallium
-  Reactor



(...sometimes in tension among themselves...)

3+1, 3+2 schemes

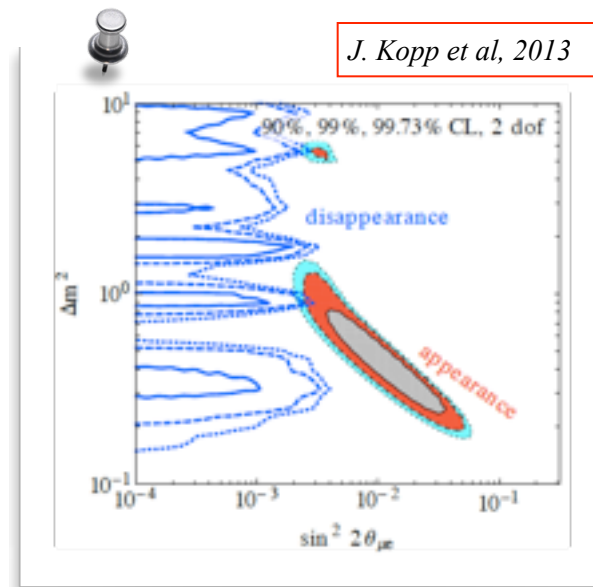
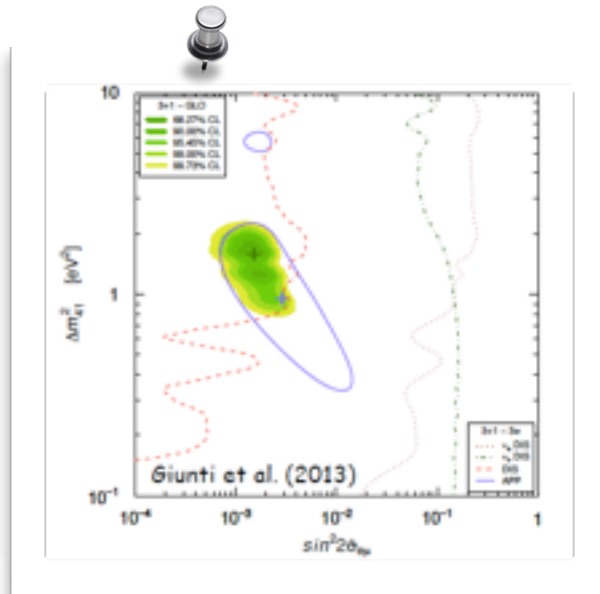
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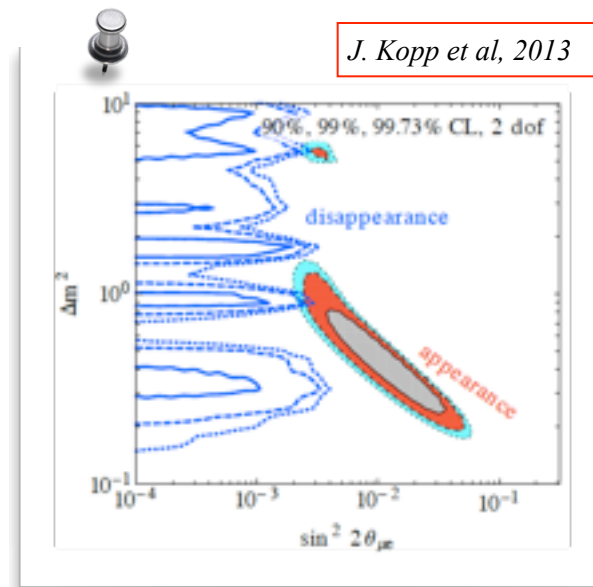
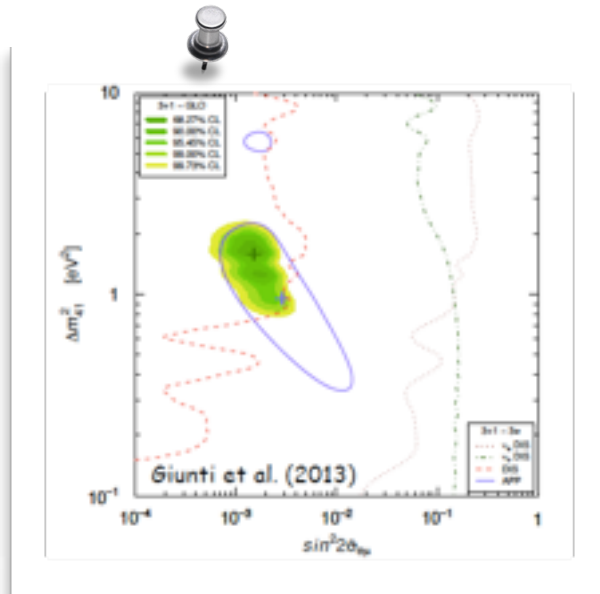
Are eV ν_s compatible with cosmology?

eV

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3+1, 3+2 schemes

Interpretation: **1** (or more) *sterile neutrino* with $\Delta m^2 \sim O$ (eV²) and $\theta_s \sim O$ (θ_{13})

Are eV ν_s compatible with cosmology?

...is necessary to assess the conditions under which they are produced

eV

Active-sterile flavour evolution

Sterile ν are produced in the Early Universe by the mixing with the active species in presence of collisions

Stodolsky, Raffelt and Sigl, 1992 ;
Sigl and Raffelt 1993;

Effects to take into account for the ν propagation:

1. Interactions with the external background medium

- Refractive effects (forward scatterings)
- Collisions which destroy the coherence of the evolution, influencing the behavior of the mixing

2. Neutrinos interactions among themselves (refractive *self-interactions*): the ν gas is so dense, that ν form a background medium, making the problem a *non-linear* phenomenon

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$$\rho_{\mathbf{p}} = \begin{pmatrix} \rho_{ee} & \rho_{e\mu} & \rho_{e\tau} & \rho_{es} \\ \rho_{\mu e} & \rho_{\mu\mu} & \rho_{\mu\tau} & \rho_{\mu s} \\ \rho_{\tau e} & \rho_{\tau\mu} & \rho_{\tau\tau} & \rho_{\tau s} \\ \rho_{se} & \rho_{s\mu} & \rho_{s\tau} & \rho_{ss} \end{pmatrix}$$

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particle distribution functions (occupation number) ➔ *flavour contents*

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➔ *sterile abundance*

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encode the phase informations
and vanish for zero mixing

Equation for the flavour evolution

Evolution equation:

$$i \frac{d\rho}{dt} = [\Omega, \rho] + C[\rho]$$

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Vacuum term

Equation for the flavour evolution

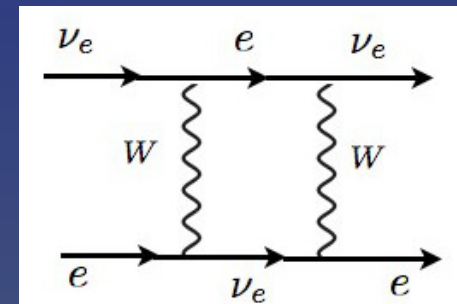
Evolution equation:

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MSW effect with background medium
(refractive effect) $\propto G_F$

→ 2th order term: “symmetric” matter effect
(charged lepton asymmetry subleading ($O(10^{-9})$))



Equation for the flavour evolution

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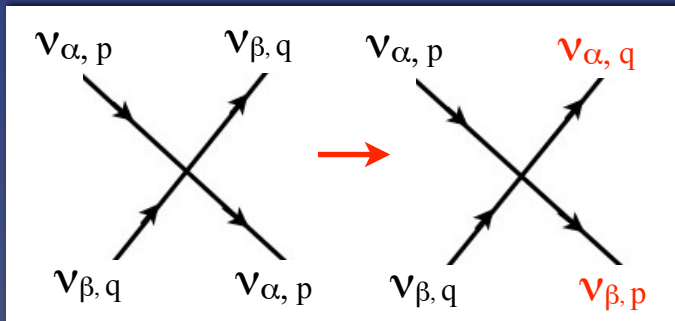
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refractive ν - ν term $\propto G_F$

self-interactions of ν with the ν background:

off-diagonal potentials \Rightarrow non-linear EoM



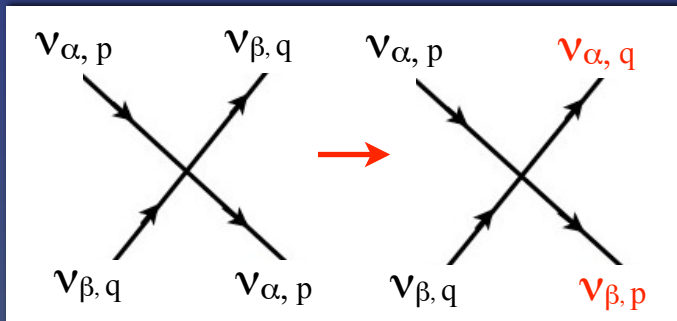
Equation for the flavour evolution

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$$i \frac{d\rho}{dt} = [\Omega, \rho] + C[\rho]$$

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$C[\rho]$

Collisional term $\propto G_F^2$

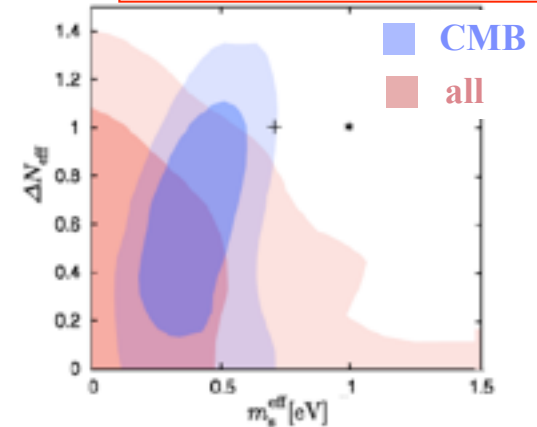
creation, annihilation and all the momentum
exchanging processes

Joint constraints on N_{eff} and Σm_ν

model	Planck +	mass bound (eV) (95% C.L.)
Joint analysis N_{eff} & 3 degen ν_a	WP+HighL+BAO	$N_{\text{eff}} = 3.32 \pm 0.54$ $\Sigma m_\nu < 0.28$
Joint analysis N_{eff} & 1 mass ν_s	WP+HighL+BAO	$N_{\text{eff}} < 3.80$ $m_{\nu_s}^{\text{eff}} < 0.42$

Planck XVI, 2013

Hamann and Hasenkamp, 2013



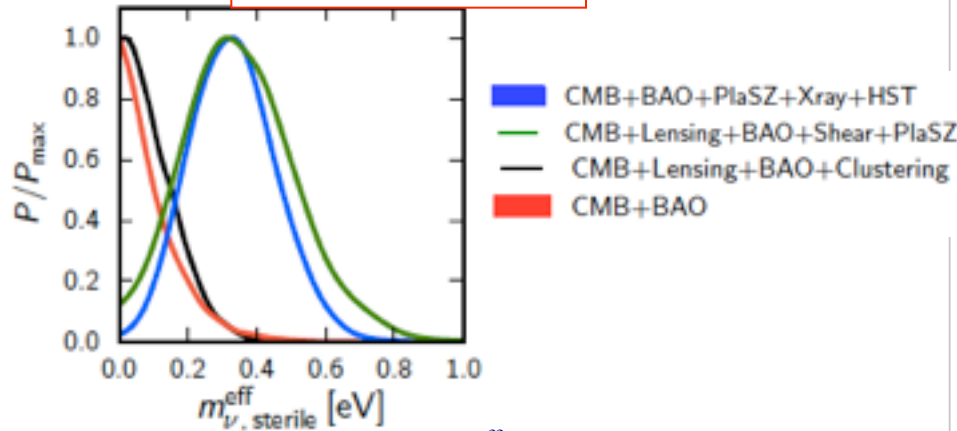
all= CMB+H0+ C+ CFHTLens

$$\Delta N_{\text{eff}} = 0.61 \pm 0.30$$

$$m_{\nu_s}^{\text{eff}} = 0.41 \pm 0.13 \text{ eV} \quad (1\sigma)$$

$$m_{\nu_s}^{\text{eff}} \equiv (94, 1 \Omega_\nu h^2) \text{ eV}$$

L. Verde et al, 2014



$$m_{\nu_s}^{\text{eff}} < 0.3 \text{ eV (95% C.L.)}$$

Bounds on active-sterile mixing parameters after Planck

- ✓ sterile abundance by flavour evolution of the active-sterile system for 3+1 scenario (to be compared with the Planck constraints)
- ✓ 2 sterile mixing angles (+ 3 active) $10^{-5} \leq \sin^2\theta_{i4} \leq 10^{-1}$ (i= 1,2)
- ✓ sterile mass-square difference $\Delta m^2_{st} = \Delta m^2_{41}$ (+ 2 active) $10^{-5} \leq \Delta m^2_{41}/eV^2 \leq 10^2$
- ✓ *average-momentum* approximation (single momentum): $\varrho_{\mathbf{p}}(T) = f_{FD}(p)\rho(T)$ ($\langle p \rangle = 3.15 T$)

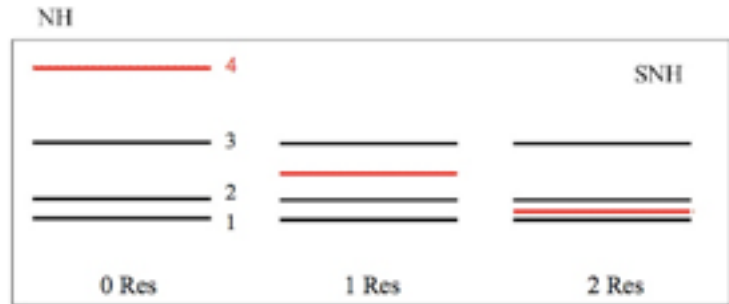
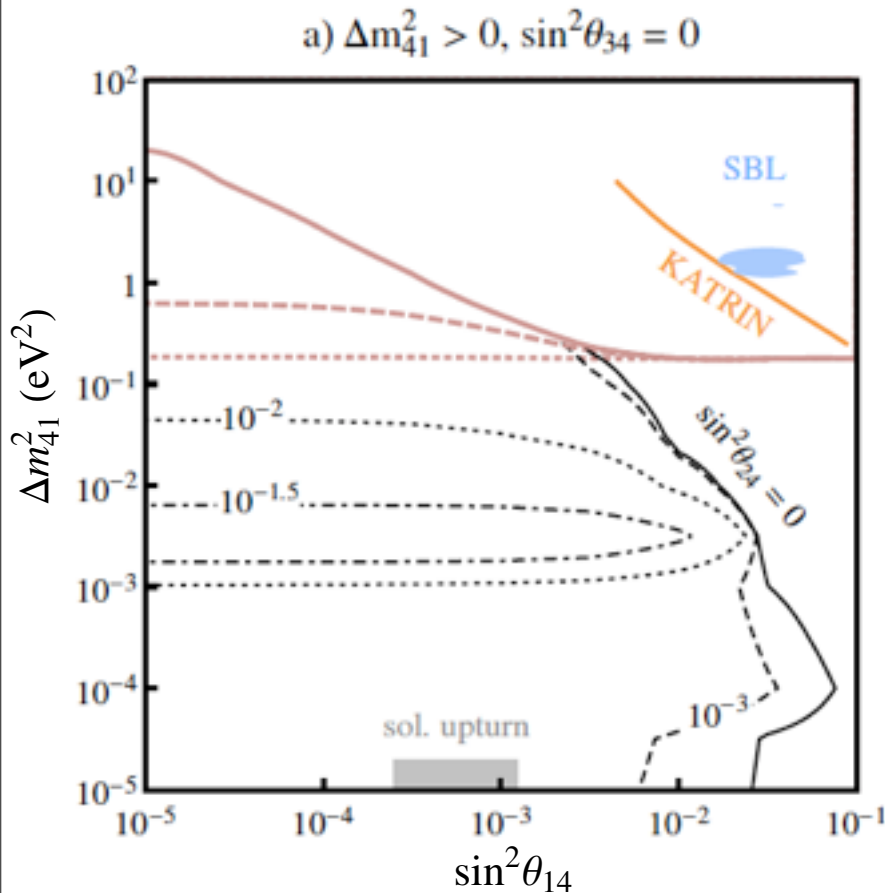
Mirizzi, Mangano, N.S. et al 2013, arXiv:1303.5368

Bounds on active-sterile mixing parameters after Planck

... our results

Mirizzi et al 2013, arXiv1303.5368

- ✓ Normal active hierarchy
- ✓ Normal sterile hierarchy



Radiation bounds

- Black curves imposing the 95% C.L. Planck constraint $N_{\text{eff}} < 3.8$ on ours $N_{\text{eff}} = \frac{1}{2} \text{Tr}[\rho + \bar{\rho}]$

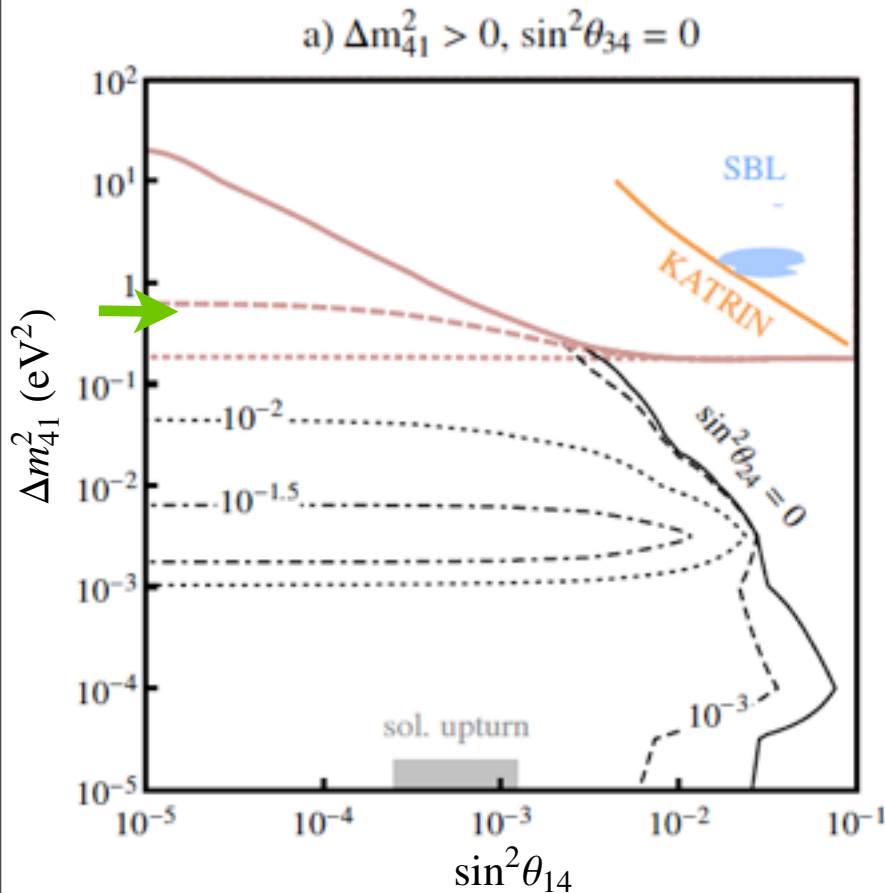
The excluded regions are those on the right or at the exterior of the black contours.

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Note: above $m \sim \mathcal{O}(1 \text{ eV})$, sterile ν are not relativistic anymore at CMB \rightarrow **NO radiation constraint**

BUT mass constraints become important

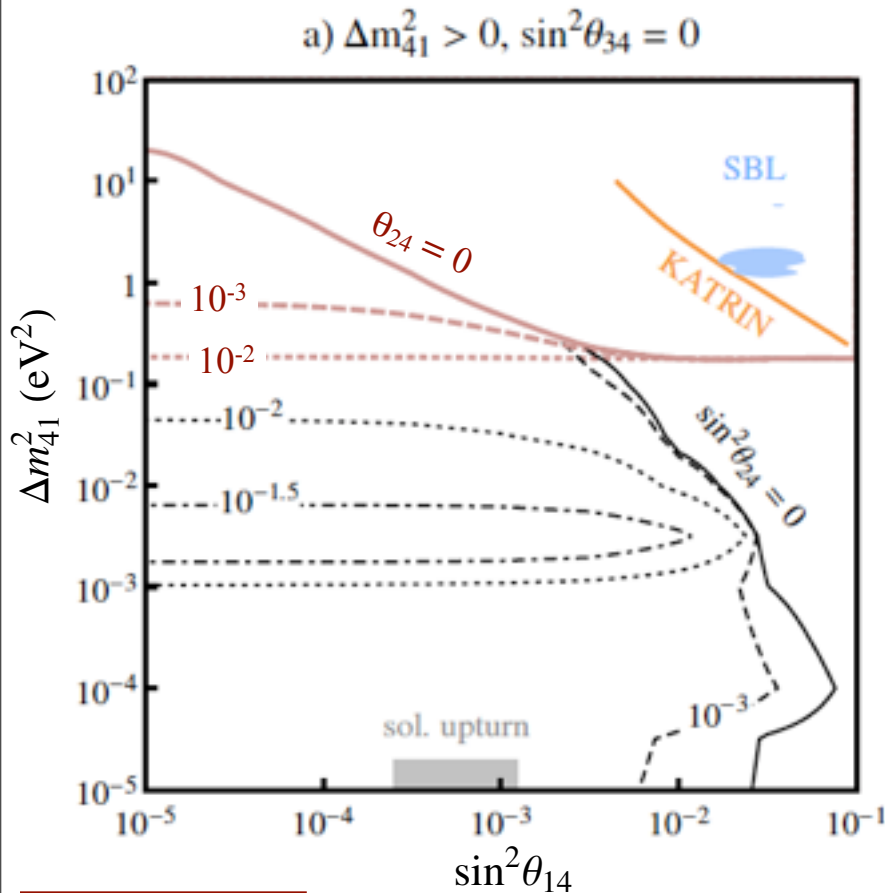


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- Red curves imposing the 95% C.L. Planck constraint $m_{\nu_s}^{\text{eff}} < 0.42 \Leftrightarrow \Omega_{\nu} h^2 < 4.5 \cdot 10^{-3}$ on ours

$$\Omega_{\nu} h^2 = \frac{1}{2} \frac{[\sqrt{\Delta m_{41}^2} (\rho_{ss} + \bar{\rho}_{ss})]}{94.1 \text{ eV}}$$

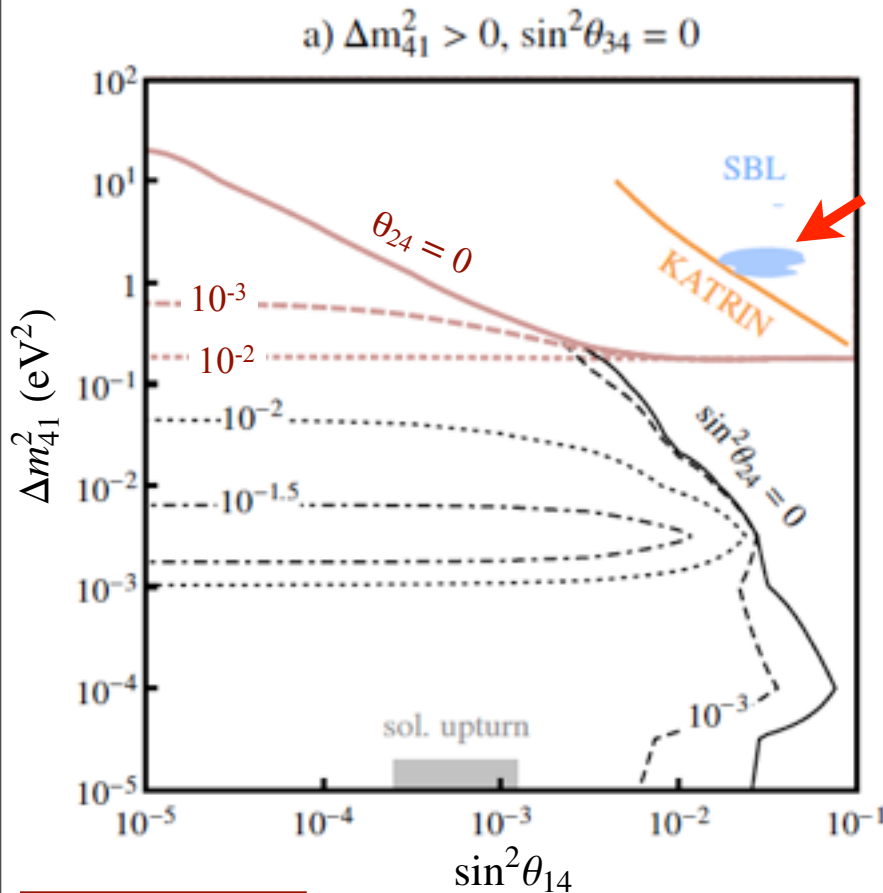
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“eV sterile ν ”
 allowed region from
 global analysis of SBL
 $\sin^2 \theta_{24} = 10^{-2}$, 95% C.L.
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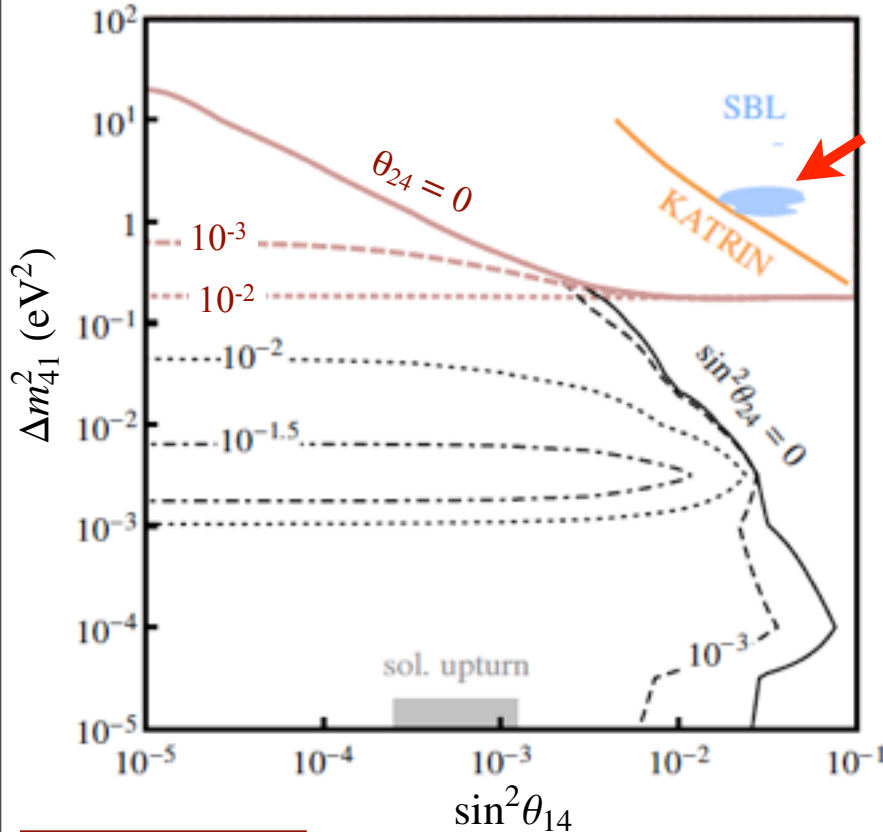
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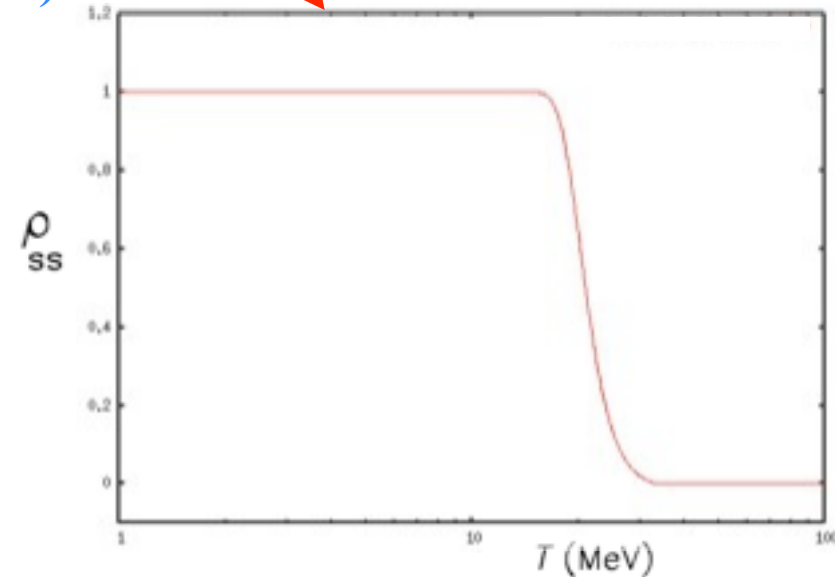
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a) $\Delta m_{41}^2 > 0$, $\sin^2 \theta_{34} = 0$



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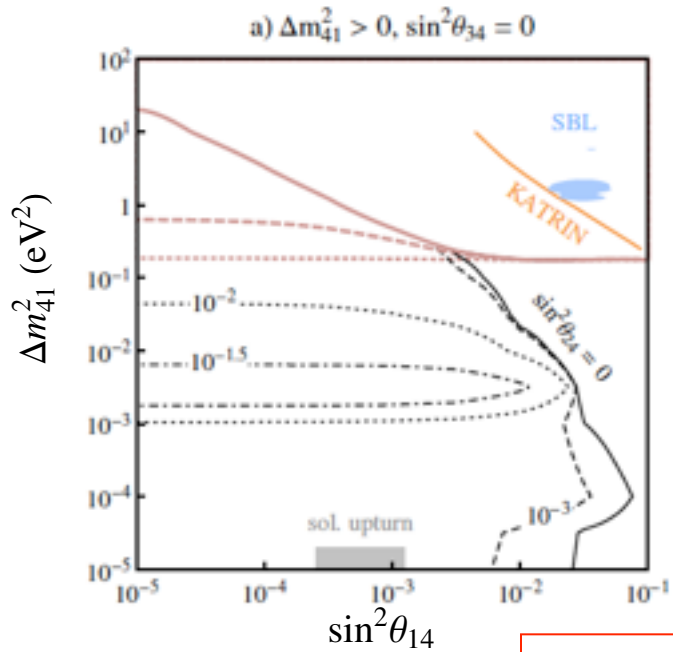
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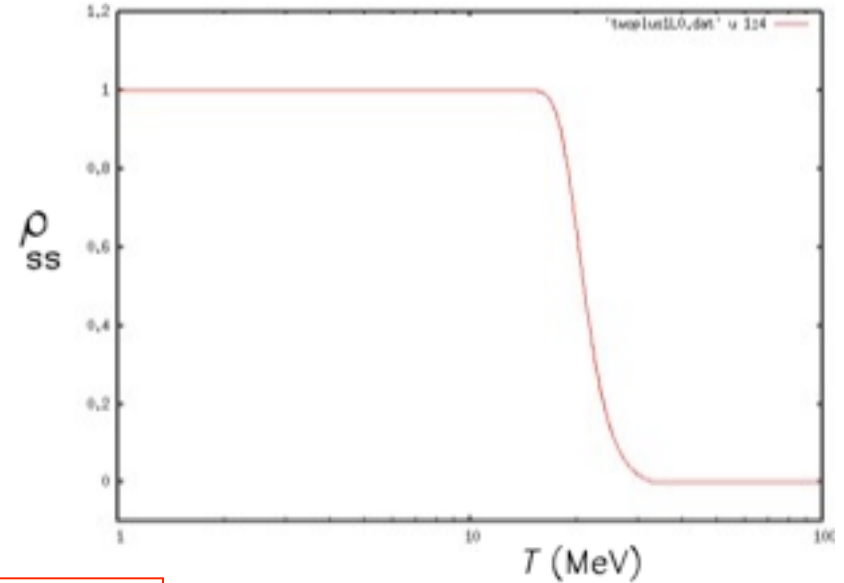
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Mirizzi et al 2013, arXiv:1303.5368

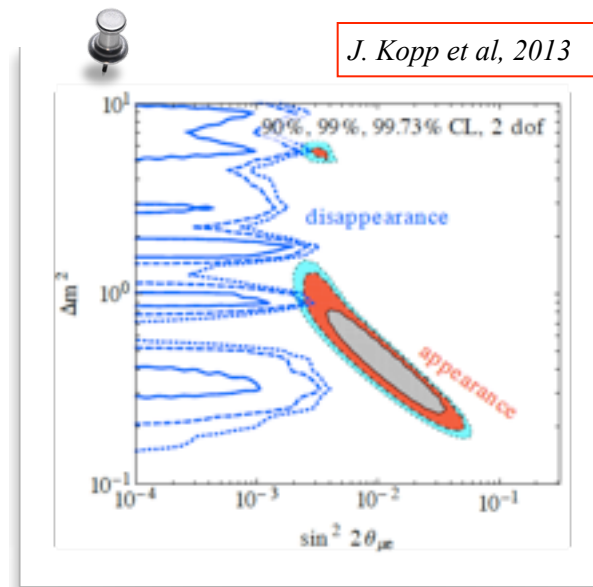
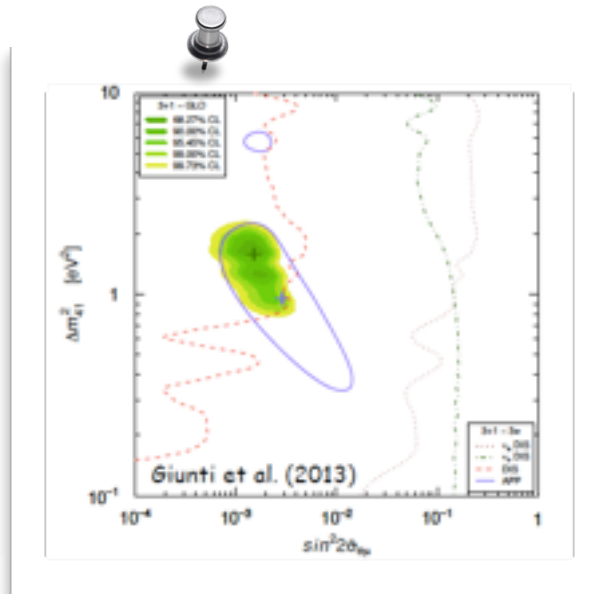


- *The sterile neutrino parameter space is severely constrained.*
- *Thermalized sterile ν with $m \sim \mathcal{O}(1 \text{ eV})$ strongly disfavored by cosmological constraints*
 - 3+1: Too *heavy* for **LSS/CMB**
 - 3+2: Too *heavy* for **LSS/CMB** and too *many* for **BBN/CMB**

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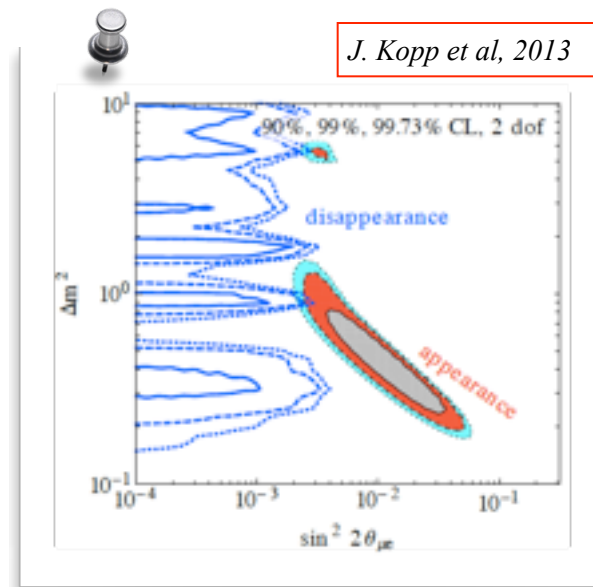
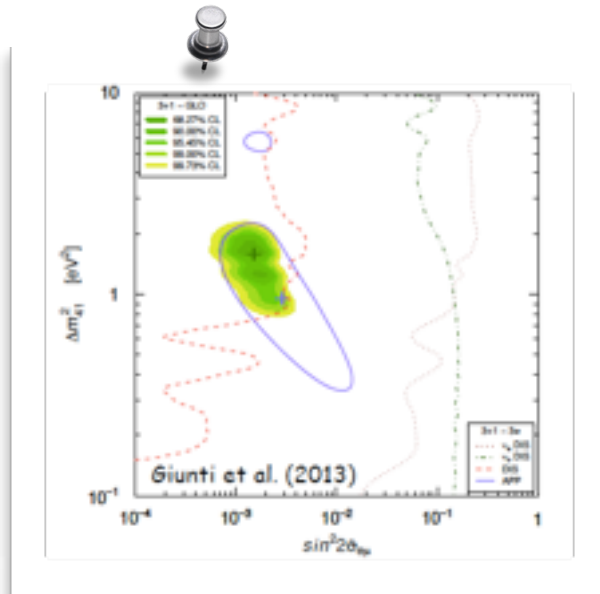
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Are eV ν_s compatible with cosmology? NO

Does exist an escape route?

eV

A possible solution: suppression of ν_s production

Different mechanisms:

1. large ν - $\bar{\nu}$ asymmetries

✓ In the presence of large ν - $\bar{\nu}$ asymmetries ($\sim 10^{-2}$) sterile production strongly suppressed. Mass bound can be evaded *Mirizzi, N.S., Miele, Serpico 2012*

⚠ Non trivial implication for BBN *Saviano et al., 2013*

2. hidden and “secret” interactions for sterile neutrinos

✓ Sterile ν feel a new potential that suppresses active-sterile mixing

⚠ Implications on BBN

⚠ Fully unconstrained model

*Hannestad et al., 2013,
Dasgupta and Kopp 2013,
Archidiacono et al., 2014*

3. low reheating scenario

✓ sterile abundance depends on reheating temperature *Gelmini, Palomarez-Ruiz, Pascoli, 2004*

⚠ simplified scenarios *Yaguna 2007*

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Sterile production with primordial neutrino asymmetry

Foot and Volkas, 1995

Introducing $L = \frac{n_\nu - n_{\bar{\nu}}}{n_\gamma}$ \rightarrow Suppress the thermalization of sterile neutrinos ($\rho_{ss} \downarrow$)
(Effective ν_a - ν_s mixing reduced by large matter term $\propto L$)

Caveat : L can also generate MSW-like resonant flavour conversions among active and sterile neutrinos enhancing their production



large L are necessary to reach the suppression

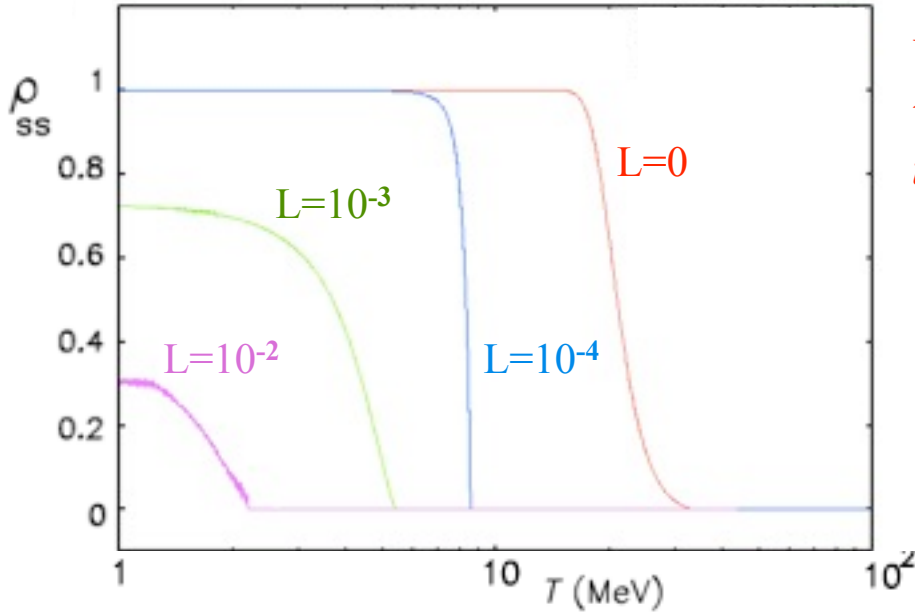
A lot of work has been done in this direction...

Enqvist et al., 1990, 1991, 1992; Foot, Thomson & Volkas, 1995; Bell, Volkas & Wong, 1998; Dolgov, Hansen, Pastor & Semikoz, 1999; Di Bari & Foot, 2000; Di Bari, Lipari and Lusignoli, 2000; Kirilova & Chizhov, 2000; Di Bari, Foot, Volkas & Wong, 2001; Dolgov & Villante, 2003; Abazajian, Bell, Fuller, Wong, 2005; Kishimoto, Fuller, Smith, 2006; Chu & Cirelli, 2006; Abazajian & Agrawal, 2008; Hannestad et al, 2012

Sterile production by neutrino asymmetry

- ✓ ρ_{ss} and distortions of ν_e spectra as function of the ν *asymmetry parameter*
→ evaluation of the cosmological consequences
- ✗ Very challenging task, involving time consuming numerical calculations
→ few representative cases

$$L_\alpha \simeq 0.68 \xi_\alpha \left(\frac{T_\nu}{T_\gamma} \right)^3$$

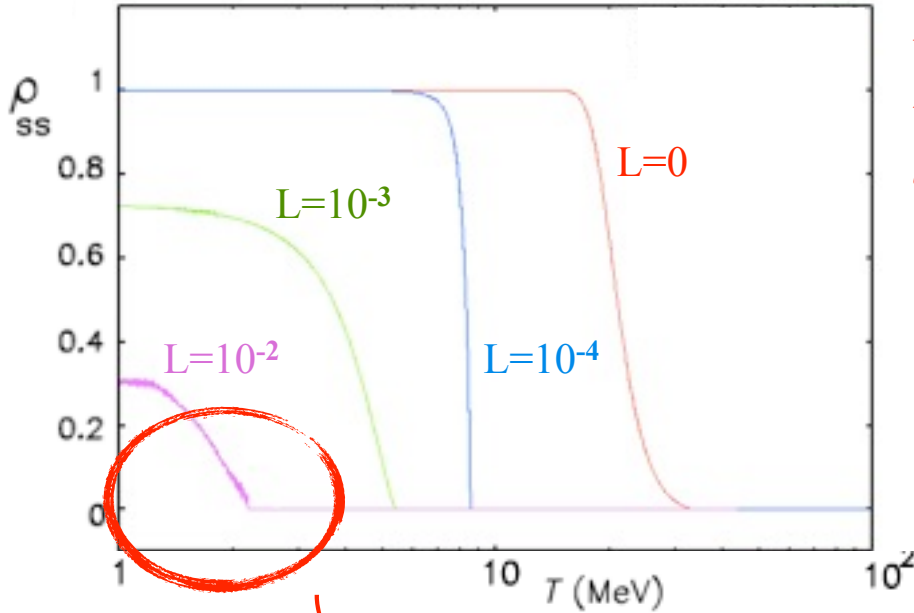


Very large asymmetries are necessary to suppress the sterile neutrino abundances leading to *non trivial consequences on BBN*

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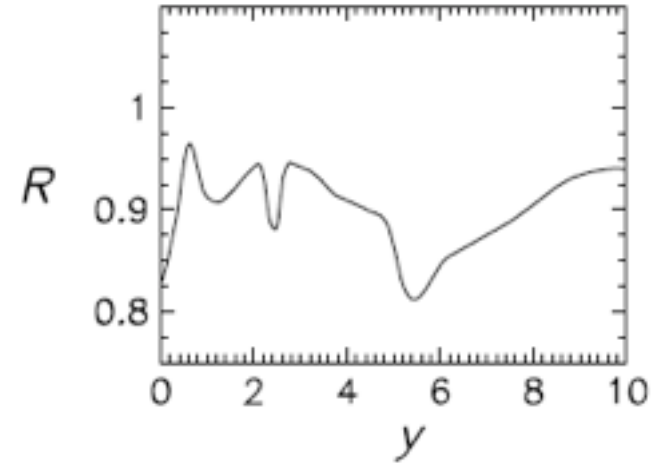
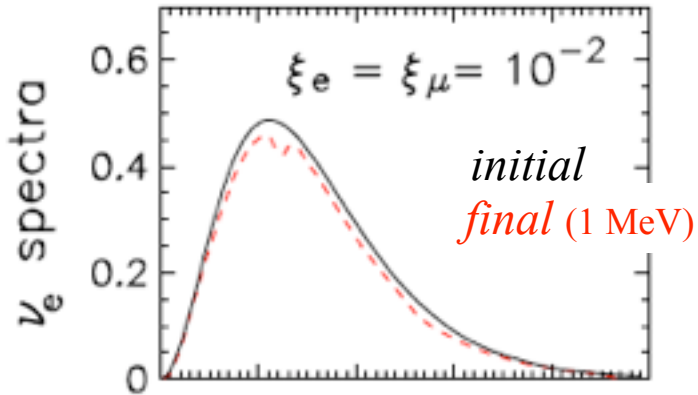
$$L_\alpha \simeq 0.68 \xi_\alpha \left(\frac{T_\nu}{T_\gamma} \right)^3$$



Very large asymmetries are necessary to suppress the sterile neutrino abundances leading to *non trivial consequences on BBN*

*conversions occur at $T \sim T_\nu$ decoupling
⇒ active not repopulated anymore by collisions ($\rho_{ee} < 1$)*

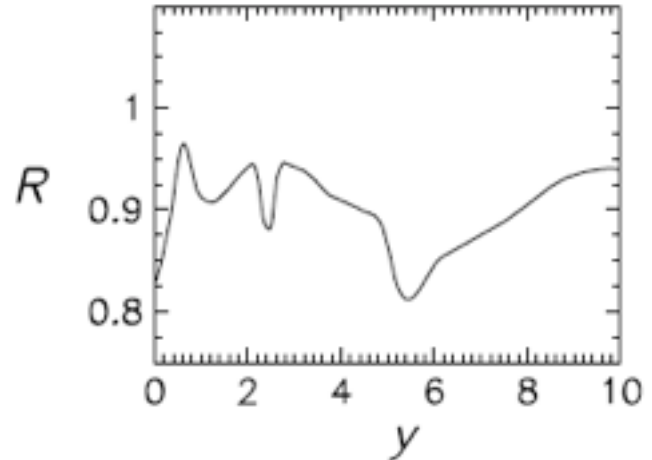
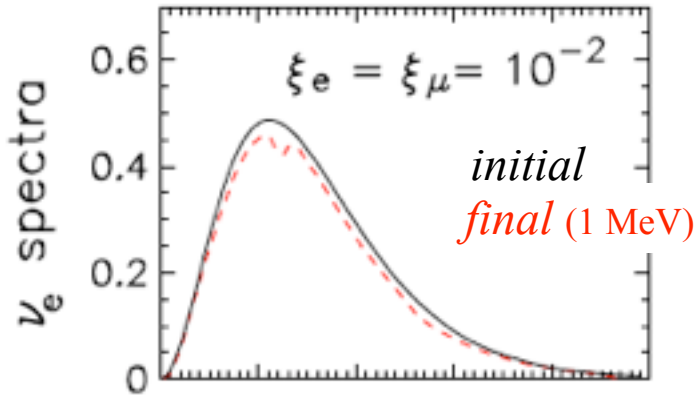
Consequences on BBN



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ν_e spectra distorted \rightarrow implications on BBN

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ν_e spectra distorted \rightarrow implications on BBN

Case	ΔN_{eff}	Y_p	$^2\text{H}/\text{H} (\times 10^5)$
$ \xi \ll 10^{-3}$	1.0	0.259	2.90
$\xi_e = -\xi_\mu = 10^{-3}$	0.98	0.257	2.87
$\xi_e = \xi_\mu = 10^{-3}$	0.77	0.256	2.81
$\xi_e = -\xi_\mu = 10^{-2}$	0.52	0.255	2.74
$\xi_e = \xi_\mu = 10^{-2}$	0.22	0.251	2.64
$\xi_e = \xi_\mu = 10^{-3}, \text{ no } \nu_s$	~ 0	0.246	2.56
$\xi_e = \xi_\mu = 10^{-2}, \text{ no } \nu_s$	~ 0	0.244	2.55
standard BBN	0	0.247	2.56

$$Y_p = \frac{2(n/p)}{1+n/p}$$

Helium mass fraction

$Y_p \uparrow$

$\text{H}^2 \uparrow$

A possible solution: suppression of ν_s production

🌐 Different mechanisms:

1. large ν - $\bar{\nu}$ asymmetries

✓ In the presence of large ν - $\bar{\nu}$ asymmetries ($\sim 10^{-2}$) sterile production strongly suppressed. Planck mass Ω_{ν} can be evaded *Mirizzi, N.S., Miele, Serpico 2012*

⚠ Non trivial implications for BBN *Saviano et al., 2013*

NOT FOR FREE

2. hidden and “secret” interactions for sterile neutrinos

✓ Sterile ν feel a new potential that suppresses active-sterile mixing

⚠ Possible implications on BBN

⚠ Fully unconstrained model

*Hannestad et al., 2013,
Dasgupta and Kopp 2013,
Archidiacono et al., 2014*

3. low reheating scenario

✓ sterile abundance depends on reheating temperature *Gelmini, Palomarez-Ruiz, Pascoli, 2004*

⚠ simplified scenarios

Yaguna 2007

Secret interactions for sterile ν_s

Hannestad, Hansen & Tram, 2013

new secret self-interactions
among sterile ν mediated by a massive
gauge boson X : $M_X \ll M_W$



*Suppress the thermalization of
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(Effective ν_a - ν_s mixing reduced by a large
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Only for sterile sector... \rightarrow *secret interactions apparently unconstrained...*

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consequences on cosmological bounds at low temperature

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If the new mediator interaction X also couples to Dark Matter \rightarrow
 \rightarrow possible attenuation of some of the small scale structure problems
("missing satellites" problem...)

Dasgupta and Kopp, 2013
Bringmann et al, 2013

Active-Sterile flavour evolution



$\nu_s - \nu_s$ interaction strength $G_X = \frac{\sqrt{2}}{8} \frac{g_X^2}{M_X^2}$ for $T \ll M_X$



2+1 scenario and single-momentum approximation: $\varrho_{\mathbf{p}}(T) \rightarrow f_{FD}(p) \rho(T)$



mass and mixing best fit parameters for active and sterile sector

(from Capozzi et al.)

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$\swarrow \propto G_F \searrow$ $\swarrow \propto G_X \searrow$

* ν asymmetry $L=0$

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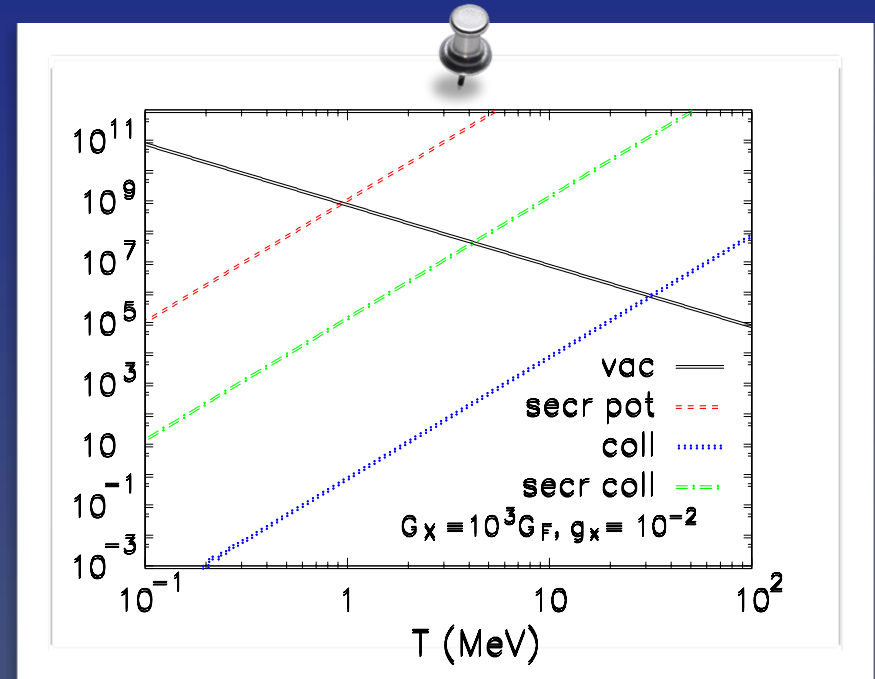
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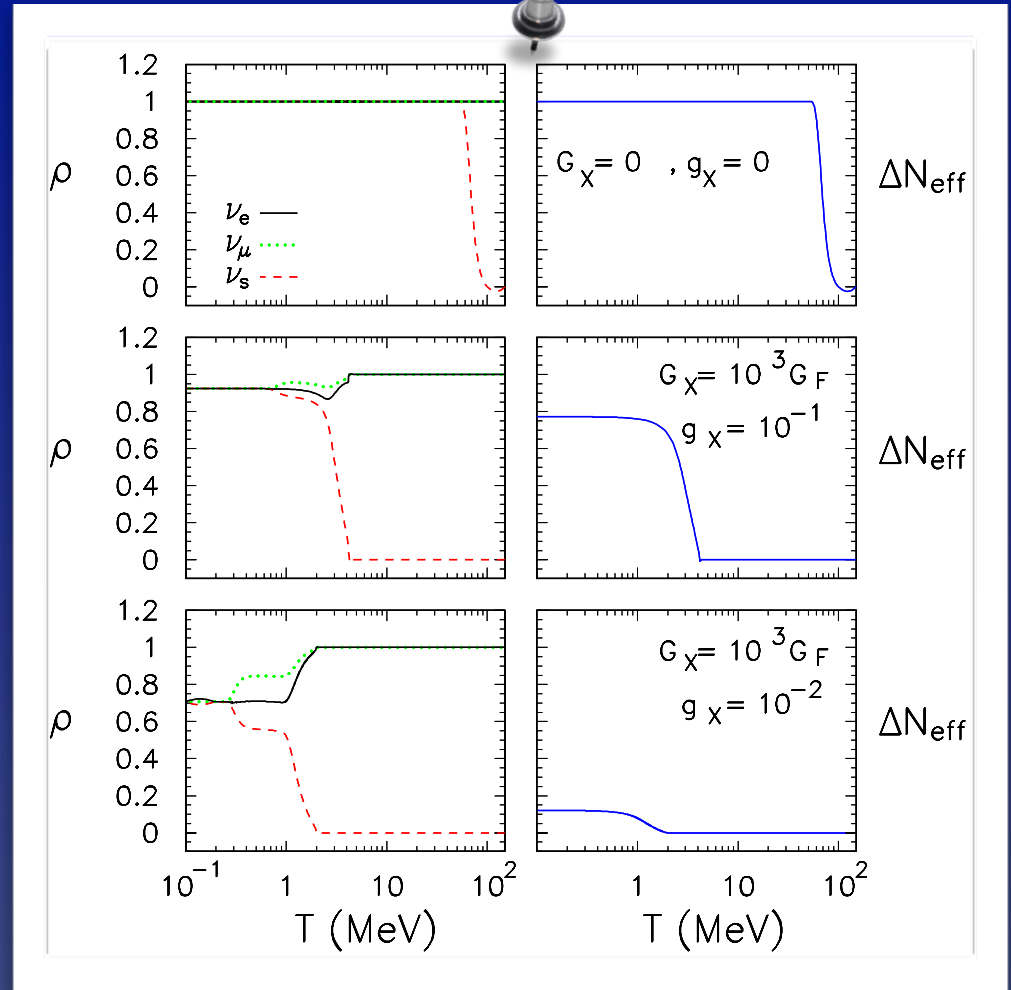
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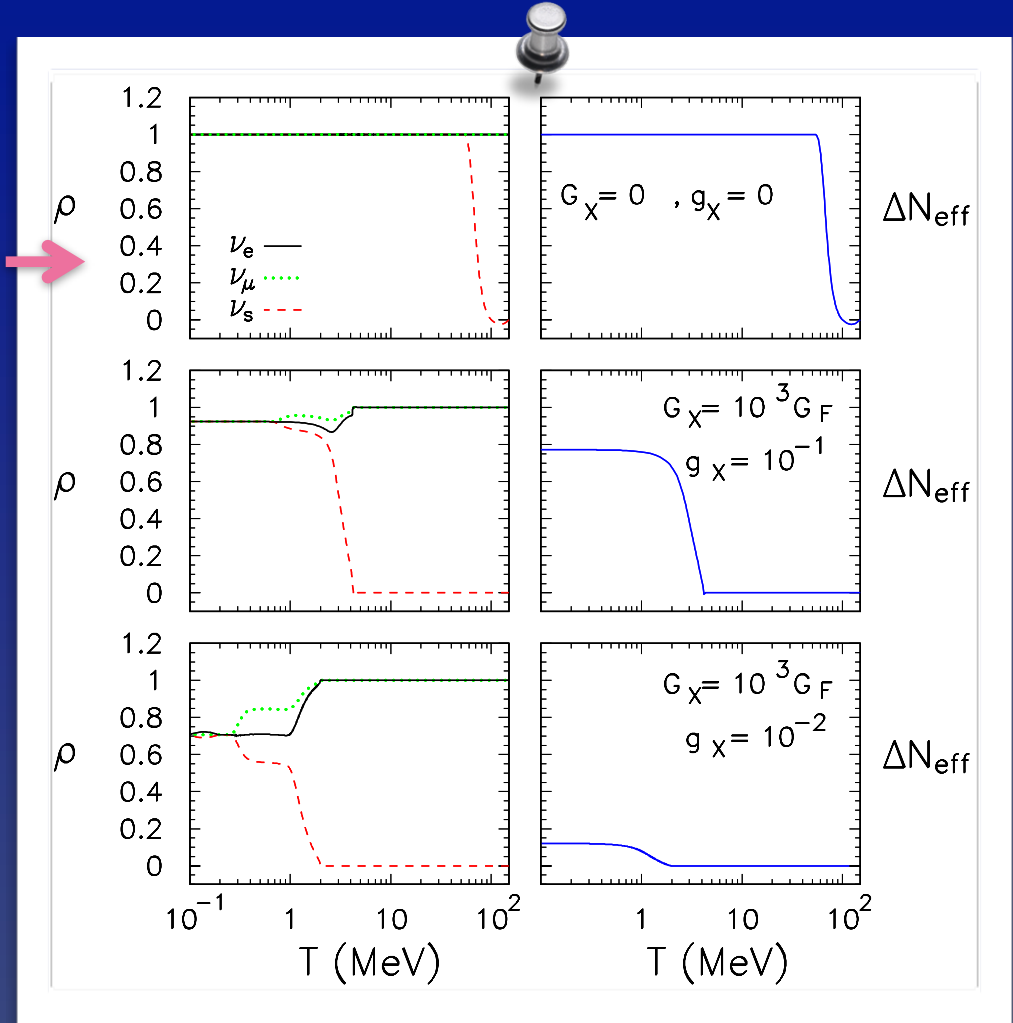
Sterile production by secret interactions



Saviano, Pisanti, Mangano, Mirizzi 2014, ArXiv: 1409.1680

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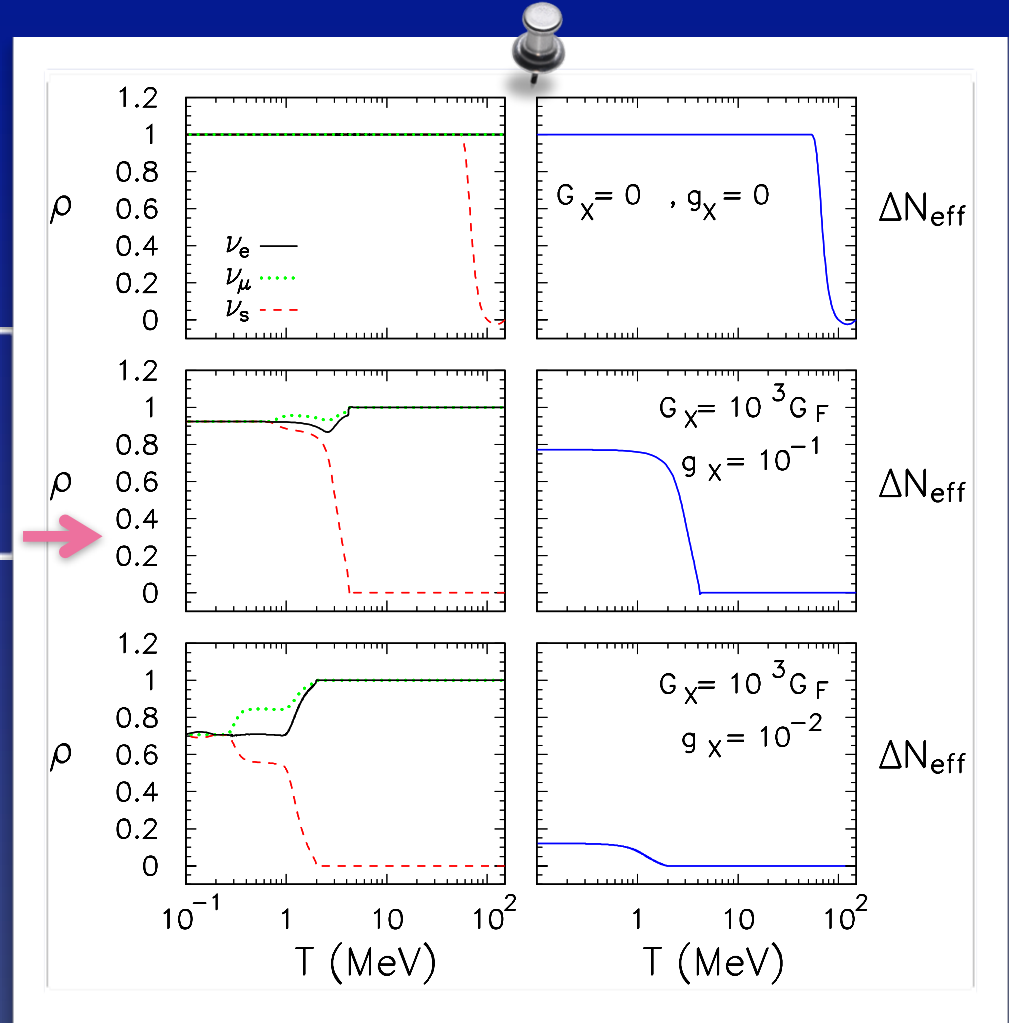
Standard case: as expected the sterile are copiously produced and thermalize



Saviano, Pisanti, Mangano, Mirizzi 2014, ArXiv: 1409.1680

Sterile production by secret interactions

Secret interactions: shift of the conversions at lower T and sterile abundance starts to be reduced

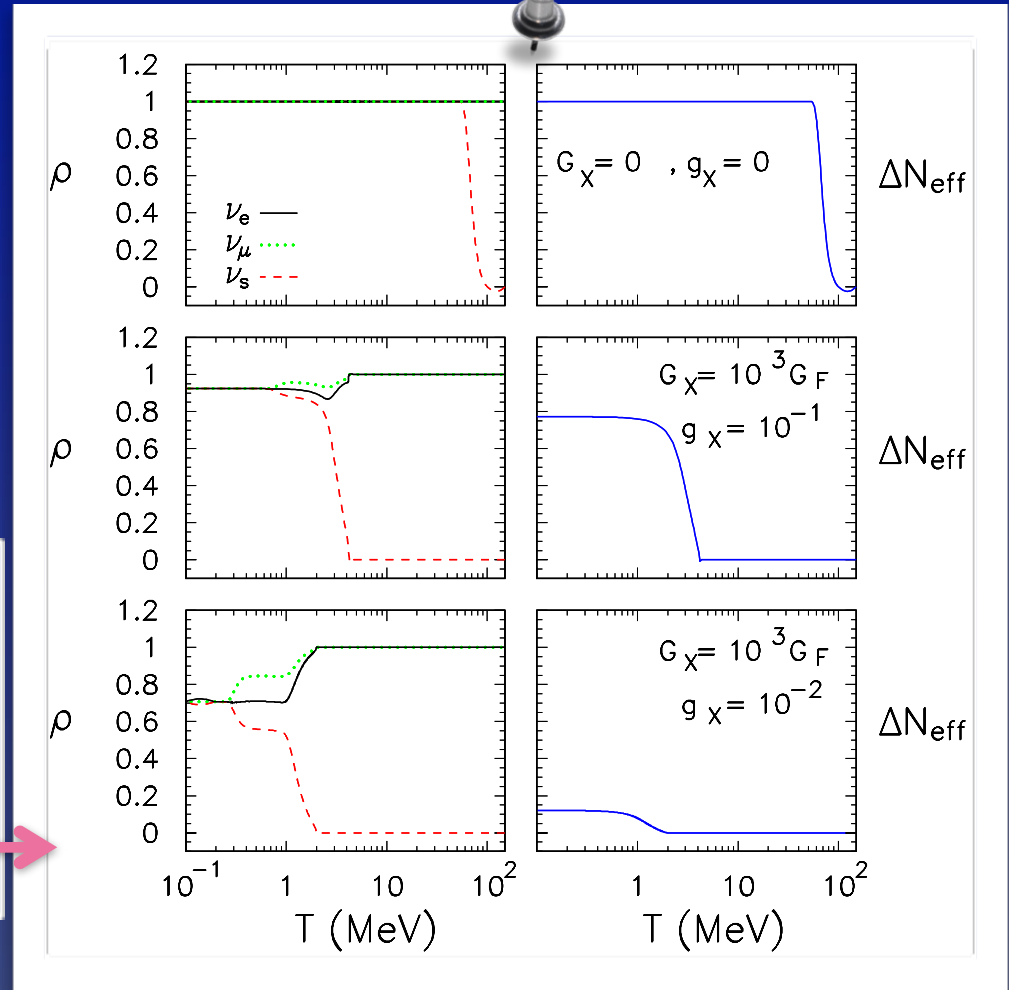


Saviano, Pisanti, Mangano, Mirizzi 2014, ArXiv: 1409.1680

Sterile production by secret interactions

Secret interactions: resonances around 1 MeV, sterile ν suppressed.
 Note that also ν_e and ν_μ the are depleted:
 crucial for N_{eff} but also for BBN

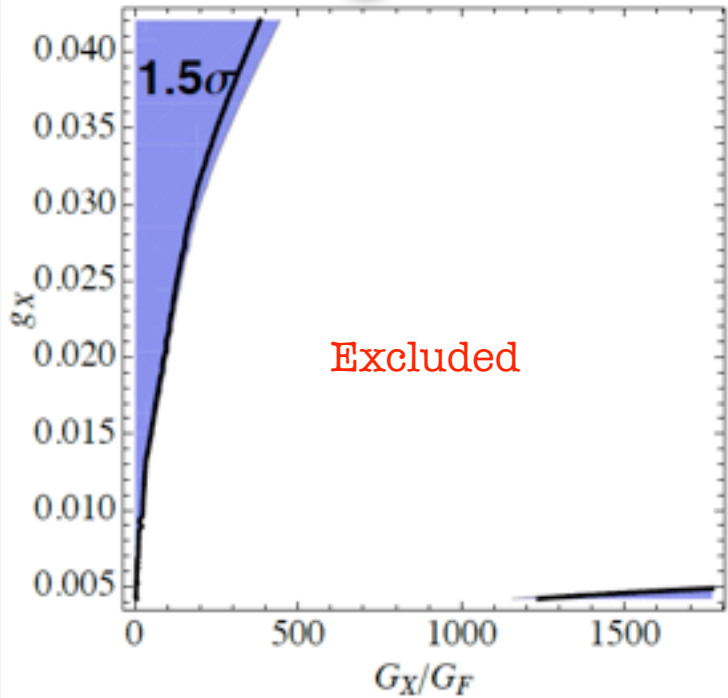
$$\rho_{ee} = 0.7, \quad \Delta N_{\text{eff}} = 0.18$$



Saviano, Pisanti, Mangano, Mirizzi 2014, ArXiv: 1409.1680

BBN constrains: primordial ^4He yield

PARthENoPE code
Pisanti et al, 2012



ΔN reduced but anyway > 0

$\rho_{ee} < 0$



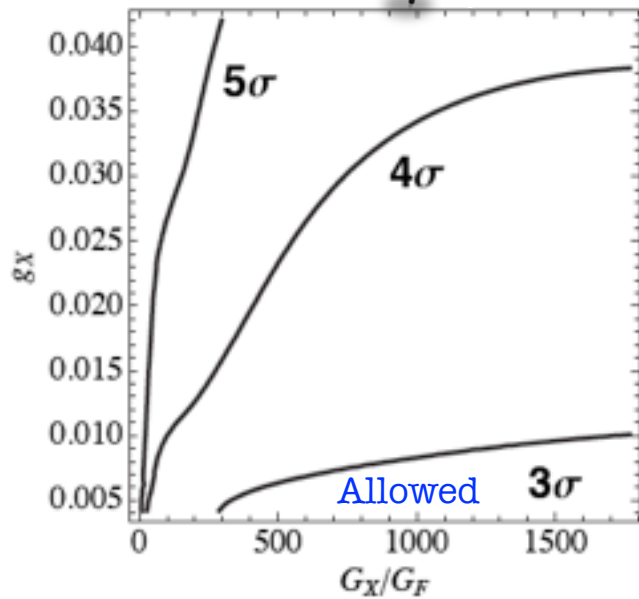
both conspire to produce a large Y_p

Experimental reference value: $Y_p = 0.2465 \pm 0.0097$

E. Aver et al, 2013
Y.I. Izotov et al, 2007

^4He analysis dominated by
the experimental error
(theoretical one extremely small)

BBN constrains: primordial ^4He yield



$$\sigma = \sqrt{\sigma_{exp}^2 + \sigma_{th}^2}$$

Planck best fit $\Omega_b h^2 = 0.02207$

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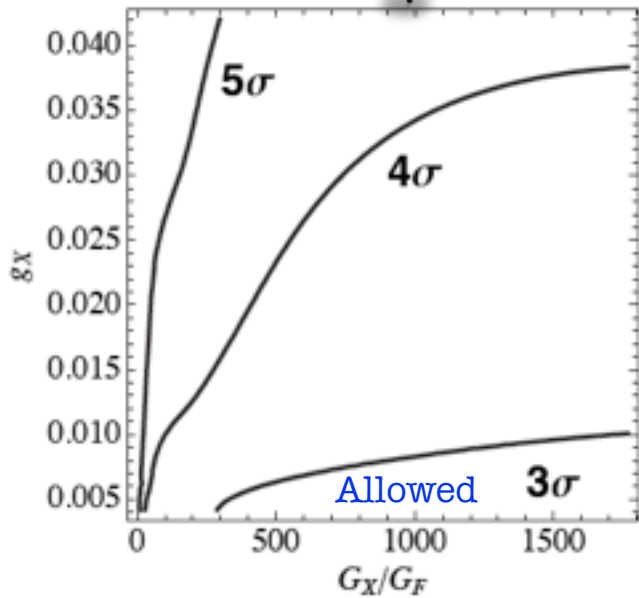
Experimental reference value: $^2\text{H}/\text{H} = (2.53 \pm 0.04) \times 10^{-5}$

R. Cooke et al, 2013

Remark: theoretical value affected by an error due mainly to the present uncertainty on the reaction $d(p, \gamma)^3\text{He} \rightarrow \sigma_{th} = 0.062 \times 10^{-5}$

Most of the parameter space excluded at $3\sigma \leftrightarrow$ mass permitted $M_X \leq 40 \text{ MeV}$

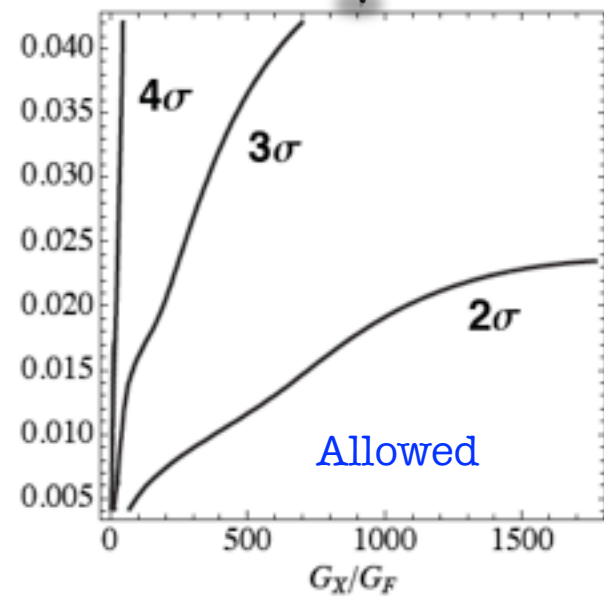
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95% C.L. Planck upper range $\Omega_b h^2 < 0.02261$

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^2H constraints weaker for larger values of $\Omega_b h^2 \leftrightarrow$ mass permitted $M_X \leq 220 \text{ MeV}$ at 3σ

Mass constraints for secret interactions

BBN can put constraints down to a mass $M_X = 40$ MeV...

... could we say something for lower masses ??

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lower $M_X \leftrightarrow$ very large $G_X (> 10^6 G_F)$



very strong secret collisional term leading to a quick flavor equilibrium

$$\text{Scattering rate: } \Gamma_X \simeq G_X^2 T_\nu^5 \frac{p}{\langle p \rangle} \frac{n_s}{n_a}$$

$$\begin{aligned} (\rho_{ee}, \rho_{\mu\mu}, \rho_{\tau\tau}, \rho_{ss})_{\text{initial}} &\longrightarrow (\rho_{ee}, \rho_{\mu\mu}, \rho_{\tau\tau}, \rho_{ss})_{\text{final}} \\ (1, 1, 1, 0) &\qquad\qquad (3/4, 3/4, 3/4, 3/4) \end{aligned}$$

Stodolsky, 1987

The flavour evolution leads to a large population of sterile states, in conflict with the cosmological mass bound

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$$m_{\text{st}}^{\text{eff}} = \rho_{ss} \sqrt{\Delta m_{\text{st}}^2} = \frac{3}{4} \sqrt{\Delta m_{\text{st}}^2}$$

lower value in the 2σ range gives $m_{\text{st}}^{\text{eff}} \sim 0.8$ eV



for the most parameter space in tension with the cosmological bounds on sterile mass (0.7 eV)

Mirizzi, Mangano, Pisanti Saviano, 2014, ArXiv:1410.1385

Cosmological constraints on secret interactions

Summarising:

- ✓ Very large $M_X \rightarrow$ thermalization of $\nu_s \leftrightarrow$ secret interactions do not have effect
- ✓ $400 \text{ MeV} < M_X < 40 \text{ MeV} \rightarrow$ severely constrained by BBN bounds
- ✓ $40 \text{ MeV} < M_X < 0.1 \text{ MeV} \rightarrow$ severely constrained by sterile mass bounds

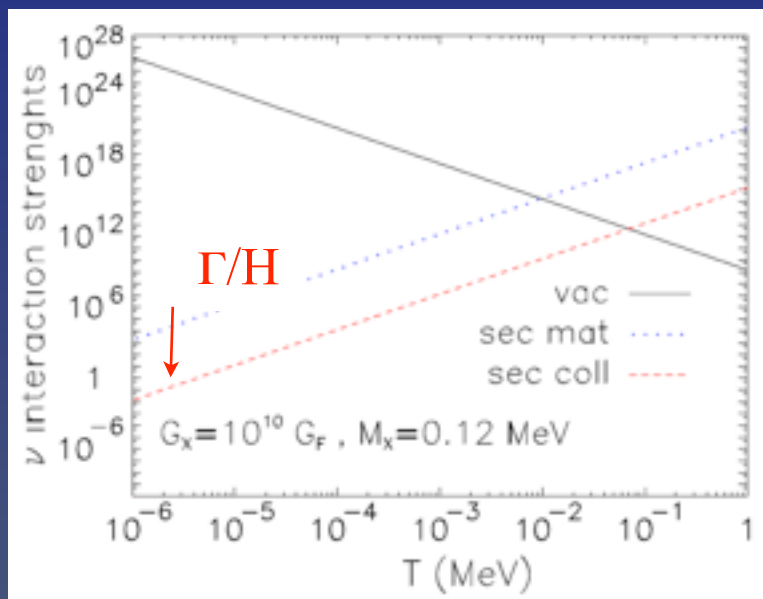
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For $M_X < 0.1 \text{ MeV} \rightarrow \nu_s$ could be still coupled at CMB and LSS epoch \rightarrow no free-streaming

Present cosmological mass bound obtained considering free-streaming ν



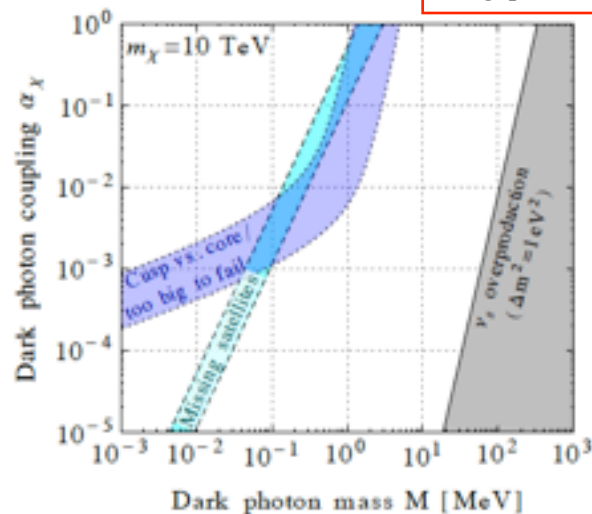
An appropriated analysis should be performed

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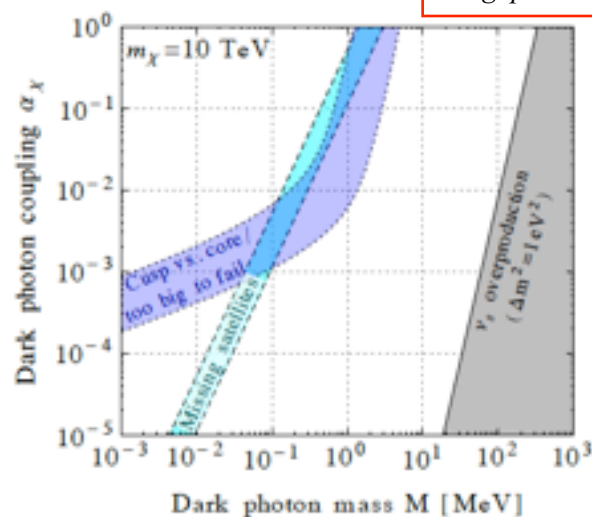
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The game is still open

A surprising feature on N_{eff}

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T_ν is reduced by a factor $(3/4)^{1/3}$,
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$$N_{\text{eff}} \sim 4 \times \left(\frac{3}{4} \right)^{4/3} \sim 2.7$$

Conclusions

- neutrino cosmology is entering the precision epoch

$$N_{\text{eff}} < 4$$

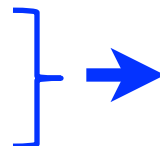
$$\Sigma_{\text{mv}} < 0.23 \text{ eV}$$

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- It is necessary to suppress the sterile production \rightarrow *exotic scenarios*

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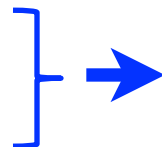
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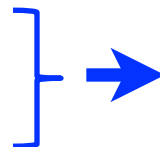
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looking forward new data...

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