



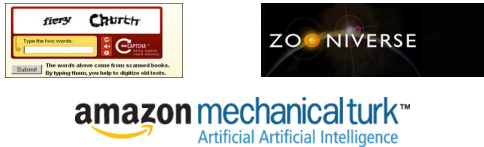
Efficient Budget Allocation with Accuracy Guarantees for Crowdsourcing Classification Tasks

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1. Motivation

Crowdsourcing systems:

Use **mass of human intelligence** to solve hard AI problems



Single response is **unreliable** \Rightarrow **redundant task allocation**

How many responses/task is **sufficient**?

- **users are paid** for their responses
- **restricted budget limit**
- budget has to be **assigned to tasks at the beginning** (online approaches are **not suitable** here)
- different tasks may provide **different payments**

2. Model Description



K **binary** classification tasks

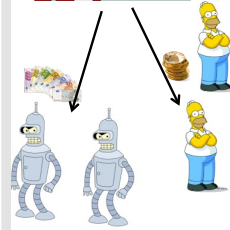
Budget limit B

Each task k :

- **unknown** ground truth $t_k \in \{0, 1\}$
- **response cost** c_k

Each user u and task k :

- response is drawn from unknown distribution



We assume that the expected response is **closer** to the ground truth

$$\mathbb{E}_{X_k} [\mu_{u,k}] = \mu_k \quad \forall k : |\mu_k - t_k| < \frac{1}{2}$$

Let $\hat{r}(n_k)$ denote the **estimate** of the truth

- derived from the received responses by using a **fusion method**

MV-efficient method: provides estimation **at least as good as** majority voting

$$\text{Estimation error } \Delta(n_k) = |\hat{r}_k(n_k) - t_k|$$

$$\text{Total exp. error } \mathbb{E}[\Delta(B)] = \sum_{k=1}^K \mathbb{E}[\Delta(n_k)] = \sum_{k=1}^K P\{\hat{r}_k(n_k) \neq t_k\}$$

Objective

Minimise the total expected error, s.t. budget limit B

Provide **theoretical performance guarantees**

4. Performance Analysis

THEOREM 1 (MAIN RESULT 1). For any $B \geq \sum_{j=1}^K c_j$, the expected estimation error of CrowdBudget is bounded as follows:

$$\mathbb{E}[\Delta(B)] \leq K e^{\frac{-2Ba^2 \min_{j=1}^K \frac{1}{c_j}}{2 \max_{j=1}^K \frac{1}{c_j}}}$$

THEOREM 2 (MAIN RESULT 2). For any $B \geq \sum_{j=1}^K c_j$ and $0 < \beta < 1$, the following bound holds for the expected estimation error of CrowdBudget with **at least $(1 - \beta)^K$** probability:

$$\mathbb{E}[\Delta(B)] \leq \max \left\{ 0, \frac{K}{2} - d_{\min} \sqrt{\frac{2B}{-\ln \frac{\beta}{2}} \sum_{j=1}^K \frac{1}{c_j}} \right\}$$

3. Algorithm

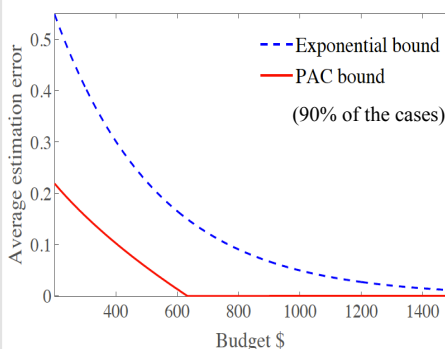
$$\text{Step 1: } n_k = \left\lfloor \frac{B}{c_k^2 \sum_{j=1}^K \frac{1}{c_j}} \right\rfloor$$

Step 2: **while** $B^r \geq 0$ **and** $k \leq K$ **do**

$$n_k = n_k + 1, B^r = B^r - c_k, k = k + 1$$

Step 3: Use an MV-efficient method to estimate responses

5. Empirical Evaluation



GalaxyZoo: 700 galaxies

- with at least 30 responses
- at least 80% consensus

Added cost to the system

